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by

John Thomas Harmond

Submitted to the Department of Ocean Engineering on May 12, 1978 in partial fulfillment of the requirements for the Degrees of Ocean Engineer and Master of Science in Naval Architecture and Marine Engineering.

ABSTRACT

A computer mathematical model that will simulate the six degree of freedom motion of a submarine has been developed. Hydrodynamic coefficients obtained from the testing of physical models enable the user to accurately simulate specific submarine designs. The simulation model can be used as a design tool to study and predict submarine dynamic response. Complete three dimensional motion is allowed for the submarine while constraints in powering, rudder deflection, dive plane angle, and response time can be selected by the user. Outputs include a chronological history of all linear and angular velocities and accelerations, the instantaneous angle of deflection of sach control surface, and the trajectory of the submarine center of gravity.

Thesis Supervisor: Martin A. Aokowitz

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Title: Professor of Ocean Engineering

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DEVELOPMENT OF A SIX DEGREE OF FREEDOM MOTION SIMULATION MODEL FOR USE IN SUBMARINE DESIGN ANALYSIS

by

John Thomas Hammond
Lieutenant, United States Navy

B.S.M.E., University of Washington (1971)

Submitted in partial fulfillment of the requirements for the degrees of

Ccean Engineer
and
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May, 1978

(5) John Thomas Hammond 1978

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Thesis Supervisor: Martin A. Abkowitz

Title: Professor of Ocean Engineering

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J.T.H.

MAY 1978
CAMBRIDGE, MASSACHUSETTS

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CHAPTER I - INTRODUCTION

I. : BACKGROUND

During the several years spent in designing a submarine, a great deal of effort is expended trying to improve the design so that the best possible vessel is eventually constructed. During the design phases the designer will frequently examine problems that were found in older submarines and try to determine the cause of each problem so that they can be eliminated in the new design. At several stages during the design, computer models are used to assist in such things as structural design, equilibrium calculations, and internal arrangement. As the design progresses, physical models of the proposed vessel are built and tested in a towing tank to measure the hydrodynamic coefficients. Finally, when it is possible to deal with the vessel as a whole, a dynamic analysis is conducted to gauge how the submarine will perform in an underwater environment when all six degrees of freedom are available.

While it is possible to gather dynamic information, such as the hydrodynamic coefficients, from physical model tests, the models are necessarily too restricted in their motion to permit a complete

analysis. It is necessary to construct a mathematical model of the submarine to simulate the submarine's motion and thereby obtain enough data for a complete analysis. The simulation model will use the hydrodynamic coefficients obtained from the physical model as a basis for the simulation. A properly constructed model will permit the designer to simulate any conceivable maneuver and gauge the submarine's response. The simulation model then becomes a tool to assist in improving the design and achieving the best possible vessel. After the submarine is designed, the model can continue to be useful by assisting in the evaluation of operating procedures. The model can be placed in any maneuvering situation without hazard to crew or vessel. This is especially useful in evaluating casualty situations. The model can also be used to estimate the effect of proposed design changes to the submarine. For instance, the model can show the effect of changing the maximum deflection of a control surface or its rate of operation.

All of the few six degree of freedom submarine simulation models in existence are too expensive for daily use in the design office. Gunerally, the models are complicated to use and sometimes difficult to obtain. These problems have created the need for a program that is both inexpensive enough to permit daily use in the design office and simple enough so that anyone can use it. This need has formed the motivation for this thesis.

I.2 MODEL DEVELOPMENT

A mathematical model must use Newton's Law of Motion and the

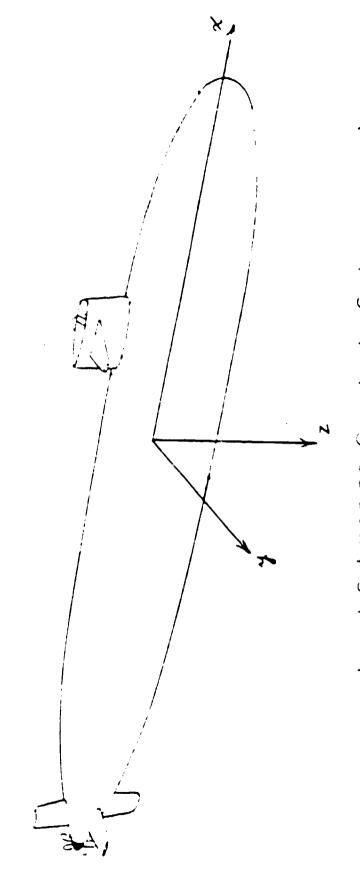
differential equations resulting from a dynamic analysis of the submarine. A submarine has movable appendages, so these must also be accounted for in the model. Newton's Law of Motion can be expressed as:

- (1) Force = $\frac{d}{dt}$ (momentum)
- (2) Howent = $\frac{d}{dt}$ (angular momentum)

If a submarine with a coordinate system such as shown in Figure 1 is used, then equation (1) can be applied along each of the three axes. Similarly, equation (2) can be applied around each axis. This gives a total of six equations to represent the six degrees of freedom of the submarine. These six equations of motion are well-known [1] so they are not developed in detail here. They are, however, included for reference in Appendix A.

while the equations of motion for the submarine form the heart of the model, they are insufficient by themselves. On an actual submarine, the officer of the deck orders the rudder or dive planes moved in order to maneuver the ship. The routines will normally sense where the ship currently is and where it is supposed to be and then move the appendages in the appropriate direction just as the deck officer would do. The six equations of motion together with the appendage control subroutines constitute the vital components of the simulation model. A main program is necessary to coordinate the input, output, and to control the action of the subroutines.

The components of the model are discussed in detail in Chapter II of this thesis. The model is written as a computer program whose features are discussed in Chapter III. The final chapter will



Local Submarine Coordinate System

Figure 1

discuss the model tests and their results. A listing of the program will be provided in Appendix B.

CHAPTER II - THE SIMULATION MODEL

II.1 GENERAL CAPABILITIES

The simulation model developed in this thesis will provide trajectory information for routine submarine maneuvers such as turning or changing depth. The trajectory, which is referenced to a fixed coordinate system, is computed as a function of time. As the trajectory of the model is developed, the velocities and accelerations are calculated and stored for output to the user. Both angular and linear velocities and accelerations are provided. The angle of deflection of each control surface appendage is computed for each step of the entire trajectory or maneuver.

The rate of deflection of each control surface and its angle of maximum deflection are specified by the user. Any of the control surfaces can be "jammed" by specifying a particular angle of deflection. The model can be initially placed on any course and depth and then ordered to come to any new course and depth. The user can select the initial speed and the appropriate thrust coefficients to cause a change in speed.

II.2 COORDINATE SYSTEMS

The coordinate system plan used in the simulation model is based on [1]. The model uses two orthogonal coordinate systems; one remaining fixed at the water surface while the other travels with the submarine to act as a local reference system. The fixed system, designated x_0 , y_0 , z_0 , is related to the moving system, designated x_0 , y_0 , z_0 , is related to the moving system, designated x_0 , y_0

The origin of the moving system is at the center of gravity of the submarine. This has the advantage that only the principal moments of inertia, I_x , I_y , I_z , are non-zero (i.e.: $I_{xy} = I_{yz} = I_{xz} = 0$). It has the additional advantage that the equations of motion in [1] also use this reference point for the x, y, x system. It would have been possible to use the centerline of the submarine for the origin. This would have the advantage of making better use of the symmetry of the vessel, however it would have the disadvantage of having to correct both the equations of motion and some of the hydrodynamic coefficients for the new origin.

Appendage movements are measured with respect to the moving coordinate system. All velocities and accelerations are measured along the axes of the moving system. This is also shown in Figure 2.

II.3 EQUATIONS OF MOTION

The general nature of the six degree of freedom model requires the use of the six equations in their non-linear form. A large

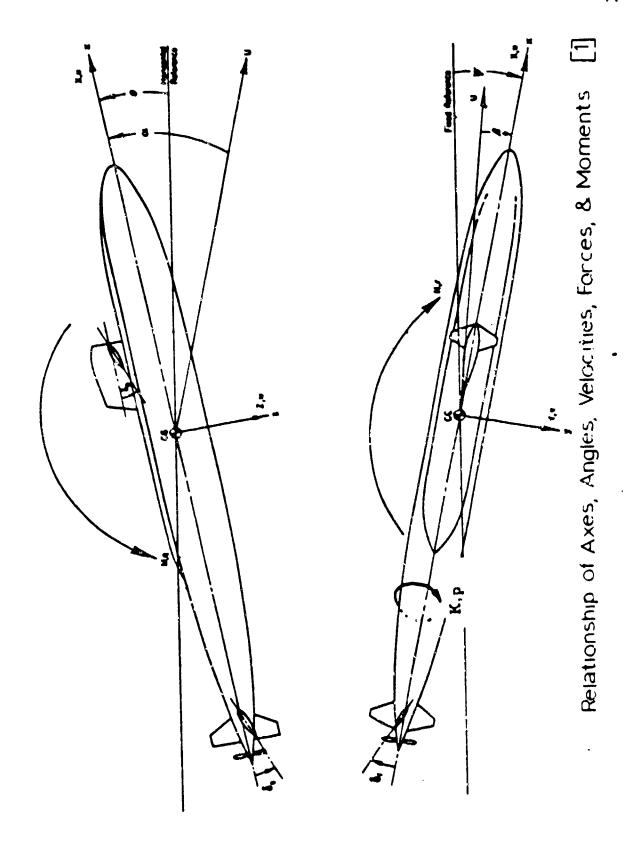


Figure 2

number of hydrodynamic coefficients are necessary for this model. It would be desirable to derive each coefficient from existing hydrodynamic theory. Some coefficients have been obtained for todies of revolution or other mathematically amenable shapes; however, when appendages such as control surfaces, fairwaters, and propellers are taken into account, the accuracy of the theoretical values is brought into question. For this reason it is standard practice to obtain the numerical value of the coefficients by experimental means. This usually entails the towing and measurement of physical models.

Once the hydrodynamic coefficients are known, the equations can be solved for the accelerations. The six equations of motion must be written such that the highest order derivatives, namely u, v, w, p, q, r and their coefficients, appear on the left hand side of the equation. This gives each equation a form like:

 $a_{1,j} = a_{1,j+1} + a_{1,j+2} + a_{1,j+2} + a_{1,j+3} + a_{1,j+4} + a_{1,j+5} + a_{1,j$

The method of solution is an iterative technique in which initial values are used in the right hand side functions and the six accelerations are solved for on the left side. The accelerations are then used to update the right side functions. A small time increment is made and the accelerations are again solved by using the latest value for the right side functions.

With each iteration the accelerations are used in a Taylor series expansion to calculate the velocities. The calculations have the form:

$$\begin{cases} L \\ d \\ b \\ d \\ d \\ d \\ d \end{cases} (\xi + 7\xi) = \begin{cases} L \\ d \\ d \\ d \\ d \\ d \\ d \end{cases} (\xi) + \begin{cases} L \\ \frac{1}{2} \\ \frac$$

The pitch, roll, and yaw argles are calculated in a similar manner using the angular velocity and acceleration.

In order to plot the trajectory of the submarine, a coordinate system transformation is performed to obtain the linear velocities x_0 , y_0 , z_0 in the fixed coordinate system. The velocities are used in a Taylor series expansion to obtain the position of the center of gravity of the submarine in the x_0 , y_0 , z_0 system.

$$\begin{cases} s^{0} \\ \lambda^{0} \\ x^{0} \end{cases} (t + 7t) = \begin{cases} s^{0} \\ \lambda^{0} \\ x^{0} \end{cases} (t) + \begin{cases} s^{0} \\ \dot{s}^{0} \\ \dot{s}^{0} \end{cases} (7t)$$

When the position of the submarine is calculated the time is advanced one increment and another iteration begins.

The iteration loop will continue to operate until some test criteria are met. For instance, if the model is performing a dive, then the model tests the value of z_0 to see if the model is at the appropriate depth. A test is also made of the pitch angle to see if it is within some specified range of zero. Lastly a check is made to ensure that all of the dive planes are at zero deflection.

II.4 CONTROL SURFACES

The motion of the model is controlled by the movement of the control surfaces. The control surfaces include the rudder, the stern planes, and the sail planes. For analysis of submarine designs the movement of the control surfaces can be governed by an automatic control system. In the model each control surface is provided with its own automatic control system. The principle of operation for all of the automatic control systems is the same. In each case the deflection of the control surface is made proportional to an error signal and the rate of change of the error. The sail planes, for instance, control the depth of the model. The calculated deflection of the planes is proportional to the depth error and the rate of change of depth.

- $\delta_c = K_1$ (present depth ordered depth)
 - + K2 (rate of change of depth)

A large error will initially cause a large deflection, but as the rate of change increases, the deflection will decrease until some moderate rate is achieved. Since movement of the sailplanes does not have any significant effect on any motion other than depth, its control system uses only the variables associated with depth.

The stern planes control pitch angle as well as depth. The control system accounts for this by using the pitch angle, θ , and the rate of change of θ .

- $\delta_c = K_3$ (present depth ordered depth)
 - + K_4 (rate of change of depth)
 - + K_c (pitch angle)
 - + K_K (rate of change of pitch angle)

The K's in the control systems are proportionality constants known as gain. The value of the gain determines the sensitivity and response of the control system. Since the error signal continually varies during a maneuver, it is best to keep the gain low. It is desirable to have just enough gain on the error signal to get the control system moving and keep it moving in the right direction. The gain on the rate signals should be much stronger to dampen out the oscillations caused by response to the error signal.

The control surfaces move at a rate specified by the user. Whenever the calculated deflection differs from the present deflection, the control surface will move toward the calculated value at the specified rate.

CHAPTER THREE - PRUGRAM USER'S GUIDE

III.1 GENERAL FEATURES

The simulation model consists of a main program and four subroutines. The four subroutines are named FUNC, RUDDER, DEPTH, and STERN. The main program reads the input data, changes units, initializes values, and prints the output. The main program performs the Taylor series expansions, the coordinate system transforms, and provides the logical statements for calling the subroutines. On the first iteration, when time equals zero, no subroutines are called; the output from this first iteration is then a statement of the initial conditions of the problem. Each succeeding iteration will call subroutine FUNC to calculate the new position of the model. Calls to the control surface subroutines are made on the basis of need, with no subroutine being called more than once in the iteration. The decision on whether or not to call RUDDER, DEPTH, or STERN is contained in a series of logical IF statements in the main program.

III.2 SUBROUTINE FUNC

Subroutine FUNC contains the six equations of motion. The

input parameters to FUNC consist of the hydrodynamic coefficients, the xidel velocities, the orientation in space, all of the ship's characteristics such as length and moments of inertia, the deflection of each control surface, and the propulsive coefficients. The subroutine returns the value of the six accelerations: UDT, VDT, WDT, PDT, QDT, RDT. The input and output for FUNC are all contained in COMMON /FOUR/ and COMMON /FIVE/. The solution to the matrix equation in subroutine FUNC is made possible by a call to the library function LEQTIF [3]. LEQTIF performs a Gaussian reduction for the matrix equation. Any similar Gaussian reduction could be substituted if LEQTIF is not available. An explanation of the parameters used in the call to LEQTIF is found in Appendix B.

111.3 SUBROUTINE RUDDER

Suproutine RUDDER controls all horizontal motion for the model. The input parameters include: K9, K10, T5, T6, T11, T12, T17, T18, TLAGR, RRATE, RUDAMT, COURSE, DELR, DELT, R, PSI. The submoutine neturns a new value for DELR, the rudder deflection, based on a calculation using its present and ordered headings. The inputs are all contained in COMMON /THREE/ and COMMON /FIVE/. Submoutine RUDDER is called whenever the model is not on the desired course or when the rudder is deflected.

III.4 SUBROUTINE DEPTH

Subroutine DEPNH controls the forward set of dive planes. It can control either box planes or sail planes depending on what the

submarine is fitted with. This subroutine is sensitive to the depth error and the rate of change of depth. Subroutine DEPTH will move the forward planes in the direction necessary to bring the depth error to zero. As input parameters, the subroutine uses: K1, K2 T1, T2, T13, T14, T15, T16, TLAGB, DELT, DIFF, ADIFF, ZDT, ATHETA, MAXANG, DCRIT. The subroutine returns a new value for DELB, the bow plane deflection, after each call.

If NAXANG, the maximum dive/ascent angle, has been exceeded, then DEPTH will return a diagnostic write statement. The user may specity MAXANG, the maximum pitch angle for the model. Whenever MAXANG is exceeded the diving planes are moved to reduce the pitch angle and a diagnostic signal is generated from within subroutine DEPTH. The diagnostic will say "Maximum dive/ascent angle exceeded at time _____. Standard fixup taken." Since the dive planes only begin to react when MAXANG is exceeded, the submarine will overshoot the angle before a reduction in the angle actually occurs. The diving planes will continue to operate until the pitch angle is less than MAXANG.

DEPTH makes only a minimal attempt to control the pitch angle of the model; it only warns the user when the angle is exceeded, and then moves the bow planes so that the pitch angle does not grow larger. The principal purpose of DEPTH is to provide depth control; it does this in conjunction with subroutine STERN.

III.5 SUBROUTINE STERN

Subroutine STERN controls the movement of the stern planes to

achieve the Kesired depth and pitch angle. The movement of the planes is sensitive to the depth error, the rate of change of depth, the pitch angle, and the rate of change of pitch. The stern planes will move to bring the depth error to zero and the pitch angle to zero. As input parameters the subroutine uses: K5, K6, K7, K8, T3, T7, T8, T10, TLAGS, STERAT, STERMX, THETA, Q, DELS, DIFF, ADIFF, ZDT, ATHETA, MAXANG, NOPICH, DCRIT. The subroutine returns a new value for the stern plane deflection, DELS. The input and output parameters are all contained in COMMON /ONE/, COMMON /FIVE/, and COMMON /SIX/. STERN is called to achieve a depth change or to correct the pitch angle.

III.6 RANGE VARIABLES

Since it is not usually possible to bring a computer simulation model to a precise depth or angle, it is necessary to define ranges around the desired depth or angle which will be acceptable to the user. For example, if the submarine were to make a depth change of 500 feet, the dive may be considered complete if the model settled within ten feet of the desired depth. The range is specified by the user to enable him to achieve whatever precision is desired. Within this range the main program will not make a call to the control surface subroutine; since no call is made, the control surfaces cannot be moved. In the program, the variable name for the depth range is NODIFF; it is usually set at \pm 5 or \pm 10 feet. Subroutine DEPTH will be called whenever the model is off of its ordered depth by more than NODIFF. The range about zero pitch angle is given the name NOPICH;

it is usually set at \pm 1 degree. STERN is called if the pitch angle is greater than NOPICH. The variable name for achieving the proper course is ONCRS; it is usually set at \pm 1 degree. RUDDER will be called whenever the model is off course by more than ONCRS.

An additional range variable is used during diving or surfacing. When the model moves within some critical range of the desired depth, it is time to begin moving the dive planes to zero angle and let the vessel glide into the desired depth. This maneuver prevents oscillation of the dive planes as the error signal and the rate signal both become small. This also ensures that the planes are at or near zero angle by the time the desired depth is reached. The name of this variable is DCRIT; it is usually set at 50, 75 or 100 feet depending on the speed of the submarine. STERN will be called whenever the model is off its ordered depth by more than DCRIT.

III.7 PROGRAM PARAMETERS

The iterative nature of the program relies on a time increment being made after each step. The size of the time increment is optional; the smaller the increment the more accurate the calculations. In selecting the size of that ime increment, one must bear in mind the length of time required to complete the maneuver and the storage capacity of the program. Jue to the quantity of information that is calculated by the program, it is practical to print only half of the data at one time. The other half of the data is stored in the array STOW. This data is then printed when the maneuver is complete.

A time check is incorporated in the main program to enable the user to limit the number of iterations. Achieving a number of iterations equal to the variable ICNT will cause the program to stop the present maneuver, print out all data, and see if another maneuver is desired. ICNT should not be made larger than 600 so that the available storage space is not exceeded.

Each control surface subroutine has a time lag scheme which senses the initial command to the control surface and prevents immediate action. A time lag occurs each time the direction of movement is changed. A different time lag may be specified for each control surface.

The variable INDEX is used to allow the user to perform more than one maneuver with a given submarine and then shift submarines to perform more maneuvers. If INDEX is less than or equal to zero then the same submarine coefficients will be used for each set of initial conditions. If INDEX is greater than zero the program will reau new coefficients as well as a new set of initial conditions.

CHAPTER FOUR - TEST RESULTS AND CONCLUSIONS

IV.1 FUNDAMENTAL MCTION TEST

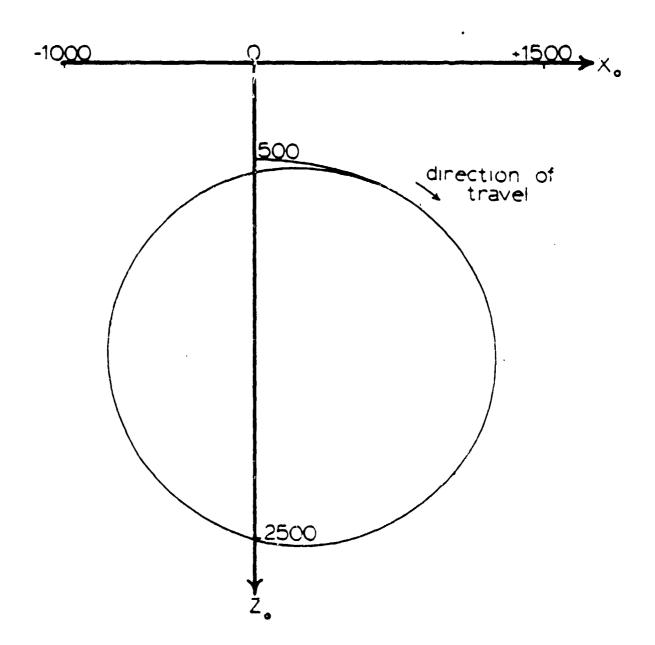
The validation of the simulation model is a matter of importance. The method used was an independent test of each component of the model, and then a series of tests with the components of the model working together. The test maneuvers were selected either because the correct dynamic response was known or because the maneuver was simple enough so that the general nature of the response could be predicted.

The first portion of the model to be tested was the subroutine FUNC. FUNC obtains the solution to the six equations of motion. It was important to establish that these equations were properly installed in the program. A test of subroutine FUNC necessitated a simultaneous test of the MAIN program to read in the hydrodynamic coefficients, set up the "A" matrix for FUNC, perform the Taylor series expansions, and write out the results. The test for FUNC was to reduce the GM of the vessel to zero and then to assume a constant angle on the dive planes. If the model was working correctly it should traverse a perfect circle in the vertical plane.

It was known that the rudder should not move and the model should not roll or yaw. The model should assume a circular trajectory with a constant angular velocity and a constant vertical component of velocity, w. Figure 3 shows the results of the maneuver. A circular trajectory was quickly achieved. The angular velocity was constant, w was constant, and the position of the model in the fixed coordinate system confirmed the circular path. The model did not roll or yaw and the rudder did not move.

IV.2 HORIZONTAL MOTION TEST

With the knowledge that the equations of motion, the Taylor series expansions, and the coordinate system transforms are operating properly, the subroutine RUDDER was the next component to test. It was decided that a simple left turn of 40 degrees would be an appropriate test. A left turn was chosen because that presents the greatest opportunity for error. The original course would be 000 degrees true and the new course would be 320 degrees true. Since the yaw angle is positive when turning right, the model must cope with a negative yaw angle as well as a proper method for dealing with course neadings given in true bearing. The subroutines DEPTH and STERN were rendered inoperative to give the opportunity of seeing RUDDER operate without interference. The model would be checked to ensure that the proper rudder rate was used and that the rudder angle did not exceed the maximum angle ordered. The model would be expected to roll and squat in the turn. A change in depth was expected since the dive planes could not act. As the model approached the new heading the



Simulation Model Trajectory With Constant Dive Plane Angle Figure 3

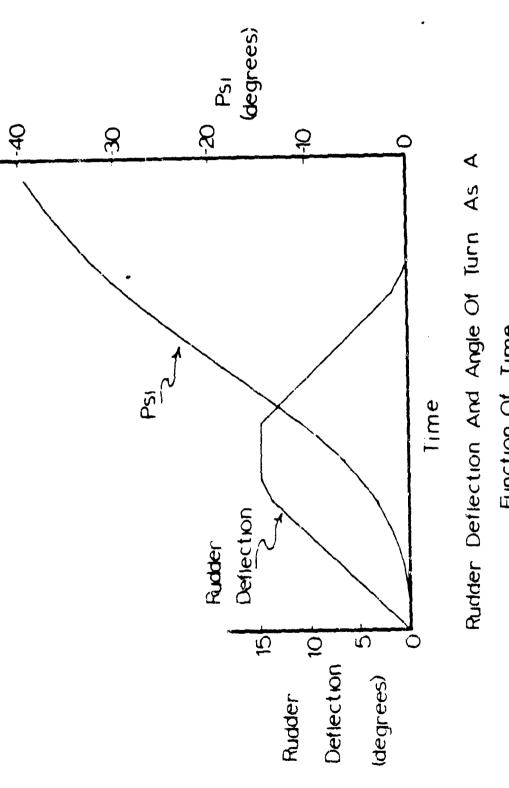
rudder should be put amidships and the vessel should steady out.

In Figure 4 the relationship between the rudder and the heading is shown as a function of time. The model reacted as predicted except possibly at the end of the turn. The rudder was amidships and the new heading was achieved but the program did not run long enough to ensure that the model was steady on the course. The model did roll, squat, and change depth as predicted. The test for RUDDER was considered to be accurate and sufficiently complete to warrant moving to the next test.

IV.3 VERTICAL MOTION TEST

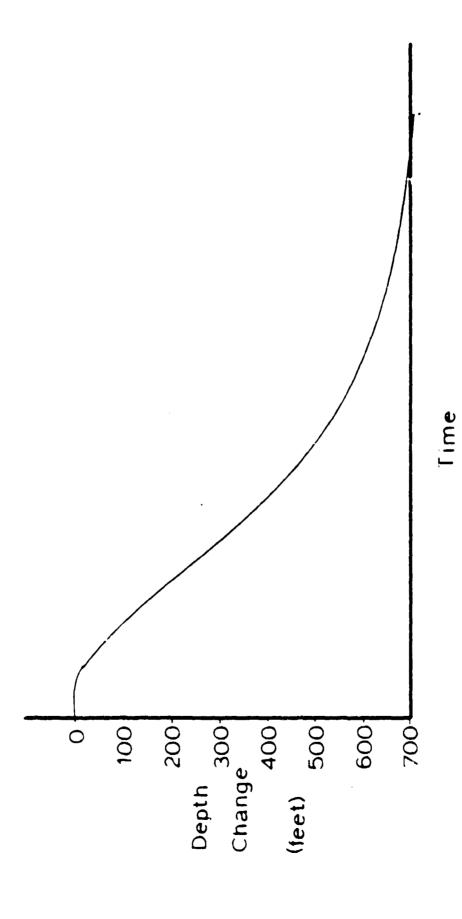
Since DEPTH and STERN operate together to regulate the depth and pitch of the model, they were tested together. The test consisted of a simple dive with a depth change of 700 feet. The course was not changed so the rudder should not move. The model should not roll or yaw. The dive planes should move in the proper direction and at the ordered rate. They should not deflect more than the ordered angle. The model should pitch downward and if the maximum ordered pitch angle is exceeded then the dive planes should move to reduce the pitch angle. As it approaches the desired depth, the model should slow its rate of descent and settle within ten feet of the depth, with $0^{\frac{a}{2}}$ 1 degree of pitch angle.

The trajectory for this test is shown in Figure 5. The model achieved steady state only six feat beyond the desired depth; the pitch angle was -.03 degrees. The dive planes were all at zero deflection. The model stayed within ten feet of the ordered depth



Function Of Time

Figure 4



The second secon

Depth As A Function Of Time For A Simple Dive

Figure 5

and within one degree of zero pitch angle for twenty seconds. This was done to ensure that a steady state had been achieved.

IV.4 COMPLETE MODEL TEST

As a final test the entire simulation model must work together. This test repeated the forty degree left hand turn but this time the dive planes were allowed to react to try to maintain the depth. The program was kept running until the pitch angle was within one degree of being zero, the model was within one degree of the proper course and the depth was within ten feet of the ordered depth. The model was initialized on course 000 degrees true at an initial speed of twenty knots.

The maneuver was successfully completed. The model remained steady at 320 -1 degrees true and the final depth was within one foot of the ordered depth. Both the pitch and roll angles were near one degree and were decreasing in magnitude. All of the control surfaces were at zero angle of deflection. It should be noted that the new course had been achieved during the first sixty seconds and that the course was maintained by the model while the proper depth and attitude were being obtained.

IV. USE AS A DESIGN TOOL

There are numerous design tasks that could be used to demonstrate the simulation model; a simple example is sufficient for this demonstration. Suppose a designer wanted to know the dynamic effects of increasing the rudder rate in a turn. The designer would elect to

use a simulation model. Since he would not want the dive planes to interfere with the analysis, he would set NODIFF, DCRIT, and NOPICH at large values so that the dive planes would not move. Then he would set RRATE, the rudder rate, at the value he desired to test and order the model to come to a new course. For this run, let's assume that the designer performed the left hand turn from 000 degrees true to 320 degrees true. He used a rudder rate of two degrees/second. He then caused the model to perform the same manuever again with a new rudder rate of four degrees/second. With the output from these two maneuvers he could easily find the time required for the turn, the advance and transfer of the submarine, and the roll and pitch angles as a function of time. The designer could use the information for whatever analysis he had in mind. The model could be run again at new rudder rates or the dive planes could be brought into play or virtually any other maneuver could be simulated. This model can also do snap roll analysis [4].

The cost of running the simulation model is so low that it can be used on a daily basis if desired. For the test turns mentioned above, the cost was less than five dollars, which included reading the cards, compilation, execution, and 900 lines of output. A designer who used the model regularly could have the model as an online dataset which would greatly reduce the cost of using the model.

IV.6 CONCLUSIONS AND RECOMMENDATIONS

This simulation model does accurately simulate the six degree of freedom motion of a submarine for moderate maneuvers. The cost of

operating the model is very low, which will allow frequent usage.

The model is designed to permit a great deal of flexibility in the application of the model. For those designers who use the simulation model, it should be a useful design tool.

If work were continued on this simulation model, it is recommended that some time be spent in improving the appendage control subroutines. Further application of control theory would be helpful with the appendage subroutines. The data input could be organized more efficiently to remove some of the opportunity for error. It could be very useful to have a plotting routine in the model to visually display the information.

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APPENDIX A

A.1 NOTATION

is inbol	Dimensionless Form	Definition
8	B' = B	Buoyancy force, positive upward
CB		Center of buoyancy of submarine
CG		Center of mass of submarine
ľ,	$I_{X_i} = \frac{\frac{1}{4} \sigma c_{\frac{1}{4}}}{I_{X_i}}$	Moment of inertia of submarine about x axis
t _y	$I_{\lambda_i} = \frac{\frac{30\pi}{L^{\lambda_i}}}{L^{\lambda_i}}$	Moment of inertia of submarine about y axis
t _a	. In's In	Moment of inertia of submarine about a axis
t _{xy}	Iny = Iny	Product of inertia about my axis
tys	$I^{\lambda x}$, $= \frac{\beta v \epsilon_x}{I^{\lambda x}}$	Product of inertia about ye axes
t _{s.x}	1 = 1 = 1 = 1 = 1 = 1 = 1 = 1 = 1 = 1 =	Product of inertia about Ex axes
ĸ	K' = K 104 UZ	Hydrodynamic moinent component about x ams (rolling moment)
ĸ"	$K_{\bullet}' = \frac{K_{\bullet}}{\frac{1}{2}\rho 4^3 U^4}$	Rolling moment when body angle (n, 3) and control surface angles are zero
κ _{•η}	K _{क्ल} ं + <u>Kee</u> हेटदे ³ U ²	Coefficient used in representing K_{α} as a function of $(\eta-1)$
ĸ	Kp' + Kp	First order coefficient used in representing K as a function of p
×	K, · · · · · · · · · · · · · · · · · · ·	Coefficient used in representing κ as a function of \hat{p}
K _{pipi}	Kpipi - Kpipi	Second order coefficient used in representing K as a function of p
K. P4	Kpq · Kpq	Coefficient used in representing K as a function of the product pq

Kqr	Kqr' + Kqr	Coefficient used in representing Kas a function of the product of
K.	K	First order coefficient used in representing K as a function of r
ĸ.	K; . 4 1966	Coefficient used in representing K as a function of F
K,	$K_{\mathbf{v}'} = \frac{K_{\mathbf{v}}}{\frac{1}{2}p\xi^2 U}$	First order coefficient used in representing K as a function of v
K +	Ky' = Ky	Coefficient used in representing K as a function of $\hat{\mathbf{v}}$
K	Ku u ' = Ku u	Second order coefficient used in representing K as a function of v
K	Knd. + for.	Coefficient used in representing K as a function of the product vq
K~~	K	Coefficient used in representing K as a function of the product $v\omega$
Kwp	Kup' = Rup	Coefficient used in representing K as a function of the product wp
X _{wf}	K	Coefficient used in representing K as a function of the product wr
K _{ir}	K	First order coefficient used in representing K as a function of δ_{p}
4	4' = 1	Overall length of submarine
m	n.' * m	Mass of submarine, including water in free-flooding spaces
M	M. + M	Hydrodynamic moment component about y axia (pitching moment)
M.	Mo	Pitching moment when body angles (g. 5) and control surface angles are zero
M _{PP}	Mpp · Mpp	Second order coefficient used in representing M as a function of p. First order coefficient is sero.
Mq	$M_{q} = \frac{M_{q}}{\frac{1}{2} \rho L^{4} U}$	First order coefficient used in representing M as a lunction of q
M ₄₇	May = May	First order coefficient used in representing Mark a function of (#-1)
мį	Ma Bock	Coefficient used in representing M as a function of à

Melel	Maial . Maial	Sucond order coefficient used in representing M as a function of q
Migiss	Migisa gpc U	Coefficient used in representing Mas as a function q
M _{rp}	Mrp' = Mrp	Coefficient used in representing Mas a function of the product rp
M _{FT}	Mrr + Mrr	Second order coefficient used in representing M as a function of r. First order coefficient is zero.
Мур	Myp' = Myp	Coefficient used in representing M as a function of the product vp
Myr	Myr' = Myr	Coefficient used in representing M as a function of the product or
M _{VV}	Myy = Myy	Second order coefficient used in representing M as a function of σ
M _w	M	First order coefficient used in representing M as a function of w
Mwŋ	Man Bold U	First order coefficient used in representing Manager as a function of (7-1)
M	Maj' + Maj	Coefficient used in representing M as a function of $\dot{\mathbf{w}}$
M(w)	M (w) * Wiw!	First order coefficient used in representing M as a function of w; equal to zero for symmetrical function
Miwiq	Mimla - Fore	Coefficient used in representing $M_{\mathbf{q}}$ as a function of \mathbf{w}
Mulul	M	Second order coefficient used in representing M As a function of w
Mujulq	$M_{w(w)\eta} = \frac{M_{w(w)\eta}}{20C^2}$	First order coefficient used in representing $M_{w/w/}$ As a function of $(\eta -1)$
M	Mww' = Mww	Second order coefficient used in representing M as a function of w. equal to zero for symmetrical function
M 9P	M36 - M36 - 106 UE	First order coefficient used in representing M as a function of $\delta_{\bf b}$
M _{ès}	$M_{3a} = \frac{M_{3a}}{604^3 U^2}$	First order coefficient used in representing M as a function of $\delta_{\frac{1}{2}}$
Мзеп	Many a For Ca	First order coefficient used in representing Mag is a function of 19-1)

и	Nr = FORTU:	Hydrodynamic moment component about a axis (yawing moment)
₩•	$N_{\bullet}' = \frac{\frac{1}{4}\rho \xi^2 U^2}{N_{\bullet}}$	Yawing moment when body ingles (g. 3) and central surface angles are zero
N _p	Nb 405. A	First order conflicient used in representing N as a function of p
N	No tota	Coefficient used in representing N as a function of $\hat{\boldsymbol{p}}$
N _{Pq}	Nad = for	Coefficient used in representing N as a function of the product pq
N _{qr}	Ngr' n yolk	Coefficient used in representing N as a function of the product or
N	N	First order lowflicient used in representing N as a function of r
N	N FM . SPECT	First order coefficient used in representing N_{ϕ} as a function of $(\gamma -1)$
NF	$N^{\frac{1}{2}} = \frac{\frac{1}{4} \Phi C_0}{N^{\frac{1}{2}}}$	Coefficient used in representing N as a function of r
Netri	Neiri - Neiri	Second refer coefficient used in representing N as a function of r
Mirise	North Party	Coefficient used in representing $N_{\delta \mathbf{r}}$ as a function of \mathbf{r}
N	$N_{\psi}^{-1} = \frac{N_{\psi}}{\frac{1}{2} p L^{2} U}$	First order coefficient used in representing N as a function of v
N	Non + Non	First order coefficient used in representing N_ϕ as a function of $(\eta-1)$
и [‡]	N°. = 187.	Coefficient axed in representing N as a function of $\tilde{\nu}$
N _M	May a Hora	Coefficient used in representing N as a function of the product vq
Nivir	Minis = Nivir	Coefficient used in representing N_{ϕ} as a function of v
Netel	Note: = Note:	Sucond order coefficient used in representing N as a function of v
Notoin	Mulvin' = Nulvin	First order coefficient used in representing $N_{\psi(\psi)}$ as a minchion of (π^{-1})

		39
N~~	N - 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	Coefficient used in representing N as a function of the product $v\mathbf{w}$
Nwp	Nup + Rup	Coefficient used in representing N as a function of the product wp
Nwr	Nur's Nur	Coefficient used in representing N as a function of the product wr
N _{br}	Nor' = 202 UT	First order coefficient used in representing N as a function of $\delta_{\rm T}$
Norn	Norn - Norn	First order coefficient used in representing $N_{\delta,r}$ as a function of $(\eta\cdot 1)$
P	p' • pl	Angular velocity component about χ axis relative to flu 4 (roll)
è	β' + β' 2 - β' 2	Angular acce eration component about x existellative to fluid
4	4. • 46	Angular velocity component about y axis relative to fluid (pitch)
4	4 . • 46.	Angular accoluration femponent about y axia relative to fluid
•	r' • ''	Angular velocity component about a ama relative to (luid (yaw)
ł	b. • <u>f.</u>	Angular acceleration component about a axis relative to fluid
U	u. • <u>n</u>	Linear velocity of origin of body axes relative to fluid
4	a. • <u>A</u>	Component of U in direction of the gazts
ů	<u>ن ۽ نوڊ</u> ريا	Time rate of change of u in direction of the maxis
^u c	- c • ' c ' ' c'	Command specific steady value of ahead speed component is for a given proreller tom when body angles (a, 3) and control surface angles are suro. Sign changes with propeller reversal
₩	₹' • Ŭ	Component of U in direction of the y axis
÷	÷. * <u>n</u>	Time rate of change of v in direction of the yaxis

		40
•	m, = <u>n</u>	Component of U in direction of the 2 axis
÷	٠ . • ١ ٥ .	Time rate of change of w in direction of the same
₩ ,	M Anton	Weight, including water in free flooding spaces
*	x. = 1	Longitudinal body axis; also the coordinate of a point relative to the origin of body axes
B	#8, # <u></u> #	The x coordinate of CB
* G	*C' * *C	The x coordinate of CG
*0	$x_0' = \frac{x_0}{\ell}$	A coordinate of the displacement of CG relative to the origin of a set of fixed axes
x	X. · X	Hydrodynamic force component along x axis (longitudinal, or exial, lorce)
×qq	x dd. = 40c.	Second order coefficient used in representing X as a function of q. First order coefficient is zero
n _{ep}	X.b Alb.	Coefficient used in representing \boldsymbol{X} as a function of the product \boldsymbol{rp}
x	$x_{rr} = \frac{x_{rr}}{9t^4}$	Second order coefficient used in representing X as a function of r. First order coefficient is term
x,	X X.	Coefficient used in representing X as a function of $\tilde{\mathbf{u}}$
Xuna	X = X	Second order coellicient used in representing X as a function of u in the non-propelled case. First order coellicient is zero
X	X vr = \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \	Coefficient used in representing X as a function of the product ve
X	X**, = \frac{\$64_1}{X^{AA}}	Second order coefficient used in representing X as a function of v. First order coefficient is zero
X	X 1041	First order coefficient used in representing $X_{\psi\psi}$ as a function of $(\eta\cdot 1)$
x _{wq}	X 4 = X 4	Coefficient used in representing \boldsymbol{X} as a function of the product we

		**
X _{ww}	Xww' - Xww	Second order coefficient used in representing X as a function of w. 'First order coefficient is zero
X	X wall = Anti	First order coefficient used in representing X_{ww} as a function of $(\eta \circ 1)$
× _{6b5b}	$X^{QPQP}, = \frac{\frac{1}{2}Df_3\Pi_3}{X^{QPQP}}$	Second order coefficient used in representing X as a function of bb. First order coefficient is zero
X _{brbr}	$X_{\delta r \delta r}' = \frac{X_{\delta r \delta r}}{\delta \rho L^2 U^2}$	Second order coefficient used in representing X as a function of δ_T . First order coefficient is zero
X _{Srbry}	X Section 2 Policy	First order coefficient used in representing $X_{\delta r \delta r}$ as a conction of $(\eta \cdot i)$
x,,,,,	$x^{9*9*} = \frac{\$ \circ \tau_* n_*}{x^{9*9*}}$	Second order coefficient used in representing X as a function of $\frac{L}{2}$. First order coefficient is zero
X 3 = 6 = 77	X Secont = Xoccon	First order coefficient used in representing X as a function of (7-1)
y	7. = 7	Lateral body axis; also the coordinate of a point relative to the origin of body axes
73	γ _B ' • '	The y coordinate of CB
7 G	7G. • <u>f</u>	The y coordinate of CG
Y _a	10, 0 10	A coordinate of the displacement of CG relative to the origin of a set of fixed axes
Y	Y' = Y	Hydrodynamic (orte component along y axis (lateral force)
۲.	$A^{\bullet_1} = \frac{\frac{4}{3}bc_1 \Omega_2}{A}$	Lateral force when body angles (a, β) and control surface angles are zero
Y _p	Yp' = Yp	First order coefficient used in representing Y as a function of p
Y	Y Y .	Coefficient used in representing Y as a function of p
Y 1 1 1 1 1 1 1 1 1	Abibi, = Abibi	Second order coefficient used in representing Y as a function of p

		46
Ypq	Abd . Abd	Coefficient used in representing Y as a function of the product pq
Yqr	Yar' . Yar	Cuefficient used in representing Y as a function of the product or
Y	$\lambda^{k}_{i} = \frac{\delta \sigma \tau_{i} \Omega}{\lambda^{k}}$	First order coefficient used in representing Y - as a function of r
Y	Try * \$24"U	First order coefficient used in representing Y_p as a function of $(\eta \cdot 1)$
Y	A Abe.	Coefficient used in representing Y as a function of $\hat{\mathbf{r}}$
Yirlar	Yirlar * Triar	Coefficient used in representing $Y_{\frac{1}{2}r}$ as a function of r
Y	4	First order coefficient used in representing Y as a function of v
Yvn	Yvn * ¥vn \$2610	First order coefficient used in representing Y_{ψ} as a function of $(\gamma -1)$
۲.	4013	Coefficient used in sepresenting Y as a function of $\hat{\mathbf{v}}$
Ywq	1 4 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	Coefficient used in representing Y as a function of the product vq
Ywirt	Ants. = 405.	Coefficient used in representing ψ as a function of \mathbf{r}
Yelei	Anial Anial	Second order coefficient used in representing Y as a function of v
Yelelm	Yululy - Tululy	First order coefficient used in representing Yuluj as a function of (n-1)
Y	Y + 104	Coefficient used in representing Y as a function of the product vw
Y	Yup' a Yup	Coefficient used in representing Y as a function of the product wp
wr	Y Ywr	Coefficient used in representing Y as a function of the product wr
T _{år}	Yer - Yer	First order coefficient used in representing Y as a function of Sr
Yen	Yarm - Yarm	First order coefficient used in representing Y as a function of (7-1)

		43
•	s. • £.	Normal body axis; also the coordinate of a point relative to the origin of body axes
*8	3B' = 3B	The a coordinate of CB
•G	•C, • ↑	The a coordinate of CG
••	r", a 40	A coordinate of the displacement of CG relative to the origin of a set of fixed axes
7.	S. = Toting	Hydron came (area component along a ama (normal (orce)
z	Z Z	Normal (orce when body angles (q, \$) and control surface angles are zero
Z pp	Z bb. = \$0f.	Second reder coefficient used in representing Z as a sunction of p. First order coefficient is zero
z _ą	$Z_q' = \frac{Z_q}{\frac{1}{2}\rho \xi^2 U}$	First or lar coefficient used in representing 2 as a function of q
Z _{qq}	Z qq' = Z qq	First order coefficient used in representing Z_{q} as a function of $(\eta \cdot 1)$
zą	Z Zi	Coefficient used in representing Z as a function of q
Ziqiss	$Z_{\text{iqi5e}} = \frac{Z_{\text{iqi5e}}}{\text{gpt}^2U}$	Coefficient used in representing $Z_{\frac{1}{2}\delta}$, as a function of q
z _{rp}	10 to 100	Coefficient used in representing Z as a function of the product rp
z _{rr}	Z rr · · · · · · · · · · · · · · · · · ·	Second order coefficient used in representing 2 as a function of r. First order coefficient is zero
=-	Z . · · · · · · · · · · · · · · · · · ·	First order coefficient used in representing 2 as a function of w
Z.	Z wy " FAL'U	First order coefficient used in representing Z_{ω} as a function of $(\eta \cdot 1)$
z.	Z Z	Coefficient used in representing Z as a function of w
Z:=(Z w · · · · · · · · · · · · · · · · ·	First order coefficient used in reprosenting Z as a function of v; equal to zero for symmetrical function
2-191	Zwiqi' = Zwiqi	Coefficient used in representing $\mathcal{Z}_{\boldsymbol{w}}$ as a function of \boldsymbol{q}

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まででは、なるまで不用のできた。までは、別は別は関係できる。 では、これでは、これでは、別は別は関係できる。までは、これできない。

	7	
Z _{wiwi}	Zwiwi - Zwiwi	Second order coefficient used in representing Z as a function of w
Lwiwin	Zwiwin · Zwiwin	First order coefficient used in representing $Z_{w[w]}$ as a function of $(\eta - 1)$
Z _{ww}	Zww = \frac{Zww}{\frac{1}{2}\ell^2}	Second order coefficient used in representing - Z as a function of w; equal to zero for symmetrical function
Z _{šb}	$Z_{\delta b}' = \frac{Z_{\delta b}}{\frac{1}{2}\rho L^2 U^2}$	First order coefficient used in representing Z as a function of $\delta_{\hat{b}}$
Z s.	Z se' = Zse iptius	First order coefficient used in representing Z as a function of δ_g
Zen	Z ten = Zoon	First order coefficient used in representing $Z_{\frac{1}{2}\alpha}$ as a function of $(\eta-1)$
•		Angle of attack
ø		Angle of druft
A _b		Deflection of bowplane or satiplane
÷,		Deflection of rudder
٨.		Deflection of sternplane
7		The ratio ue
•		Angle of pitch
•		Angle of yaw
•		Angle of roll
a ₁ , b ₁ , c ₁		Sets of constants used in the representation of propeller thrust in the axial equation

A.2 EQUATIONS OF NOTION AXIAL FORCE

LATERAL FORCE

$$\begin{split} & m \left[\dot{v} - wp + ur - y_G \left(r^2 + p^2 \right) + z_G \left(qr - p \right) + x_G \left(qp + \dot{r} \right) \right] = \\ & + \frac{o}{2} L^4 \left[Y_r^{-1} \dot{r} + Y_p^{-1} \dot{p} + Y_{-p|p|}^{-1} p_{|p|} + Y_{pq}^{-1} p_{|p|} + Y_{qr}^{-1} qr \right] \\ & + \frac{o}{2} L^2 \left[Y_v^{-1} \dot{v} + Y_{vq}^{-1} vq + Y_{wp}^{-1} wp + Y_{wr}^{-1} wr \right] \\ & + \frac{o}{2} L^2 \left[Y_r^{-1} ur + Y_p^{-1} up + Y_{-|r|\delta r}^{-1} u|r|5r + Y_{v|r|}^{-1} \frac{v}{|v|} |(v^2 + w^2)^{\frac{1}{2}} ||r|| \right] \\ & + \frac{o}{2} L^2 \left[Y_w^{-1} u^2 + Y_v^{-1} uv + Y_{v|v|}^{-1} v + |(v^2 + w^2)^{\frac{1}{2}} \right] \\ & + \frac{o}{2} L^2 \left[Y_{vw}^{-1} vw + Y_{5r}^{-1} u^2 \delta r \right] \\ & + (W - B) \cos \theta \sin \theta \\ & + \frac{o}{2} \mathcal{E}^3 Y_{r\eta}^{-1} ur (\eta - 1) \\ & = \frac{o}{2} \mathcal{E}^3 Y_{v\eta}^{-1} ur + Y_{v'v|\eta}^{-1} v + (v^2 + w^2)^{\frac{1}{2}} + Y_{5r\eta}^{-5} u^2 \right] (\eta - 1) \end{split}$$

NORMAL FORCE

ROLLING MOMENT

$$\begin{split} & I_{x} \dot{p} + (I_{z} - I_{y}) \, qr - (\dot{r} + pq) \, I_{xz} + (r^{2} - q^{2}) \, I_{yz} + (pr - \dot{q}) \, I_{xy} \\ & + im \left[y_{G} \, (\dot{w} - uq + v\rho) - z_{G} \, (\dot{v} - wp + ur) \, \right] = \\ & + \frac{\theta}{2} \, L^{0} \left[K_{p}^{-1} \dot{p} + K_{p}^{-1} \dot{r} + K_{qr}^{-1} \, qr + K_{pq}^{-1} \, pq + K_{p|p|}^{-1} p|p| \right] \\ & + \frac{\theta}{2} \, L^{4} \left[K_{p}^{-1} \, up + K_{r}^{-1} \, ur + K_{v}^{-1} \dot{v} \, \right] \\ & + \frac{\theta}{2} \, L^{4} \left[K_{vq}^{-1} \, vq + K_{wp}^{-1} \, wp + K_{wr}^{-1} \, wr \, \right] \\ & + \frac{\theta}{2} \, L^{3} \left[K_{w}^{-1} \, u^{2} + K_{v}^{-1} \, uv + K_{v|v}^{-1} \, v|(v^{2} + w^{2})^{\frac{1}{2}} \, \right] \\ & + \frac{\theta}{2} \, L^{3} \left[K_{vw}^{-1} \, vw + K_{3r}^{-1} \, u^{2} \, \delta r \, \right] \\ & + (y_{G} \, W - y_{B} \, B) \, \cos \, \theta \, \cos \, \phi - (z_{G} W - z_{B} B) \, \cos \, \theta \, \sin \, \phi \, \right] \\ & + \frac{\theta}{2} \, \ell^{3} \, K_{\phi \eta}^{-1} \, u^{2} \, (\eta - 1) \end{split}$$

PITCHING MOMENT

$$\begin{split} & I_{y} \dot{q} + (I_{x} - I_{x}) rp - (p + qr) I_{xy} + (p^{2} - r^{2}) I_{xx} + (qp - r) I_{yx} \\ & + m \left[z_{G} \left(\dot{u} - vr + wq \right) - x_{G} \left(\dot{w} - uq + vp \right) \right] z \\ & + \frac{p}{2} I^{a} \left[M_{q}^{'} \dot{q} + M_{pp}^{'} p^{2} + M_{rr}^{'} r^{2} + M_{rp}^{'} rp + M_{q|q|}^{'} q|q| \right] \\ & + \frac{p}{2} I^{a} \left[M_{w}^{'} \dot{w} + M_{vr}^{'} vr + M_{vp}^{'} vp \right] \\ & + \frac{p}{2} I^{a} \left[M_{q}^{'} \dot{u} + M_{|q|} \delta s^{'} \dot{u}|q| \delta s + M_{|w|q}^{'} |(v^{2} + w^{2})^{\frac{1}{2}} |q| \right] \\ & + \frac{p}{2} I^{a} \left[M_{q}^{'} \dot{u} + M_{w}^{'} \dot{u} + M_{w|w}^{'} |w| (v^{2} + w^{2})^{\frac{1}{2}} \right] \\ & + \frac{p}{2} I^{3} \left[M_{|w|}^{'} \dot{u}|w| + M_{ww}^{'} |w| (v^{2} + w^{2})^{\frac{1}{2}} \right] \\ & + \frac{p}{2} I^{3} \left[M_{vv}^{'} \dot{v}^{2} + M_{5s}^{'} \dot{u}^{2} \delta s + M_{5b}^{'} \dot{u}^{3} \delta b \right] \\ & - (x_{G} W - x_{B} B) \cos \theta \cos \phi - (z_{G} W - z_{B} B) \sin \theta \\ & + \frac{p}{2} \ell^{4} M_{q\eta}^{'} \dot{u} \dot{q} (\eta - 1) \\ & + \frac{p}{2} \ell^{3} \left[M_{w\eta}^{'} \dot{u} \dot{q} (\eta - 1) \right] \\ & + \frac{p}{2} \ell^{3} \left[M_{w\eta}^{'} \dot{u} \dot{q} (\eta - 1) \right] \\ & + \frac{p}{2} \ell^{3} \left[M_{w\eta}^{'} \dot{u} \dot{q} (\eta - 1) \right] \\ & + \frac{p}{2} \ell^{3} \left[M_{w\eta}^{'} \dot{u} \dot{q} (\eta - 1) \right] \\ & + \frac{p}{2} \ell^{3} \left[M_{w\eta}^{'} \dot{u} \dot{q} (\eta - 1) \right] \\ & + \frac{p}{2} \ell^{3} \left[M_{w\eta}^{'} \dot{q} \dot{q} (\eta - 1) \right] \\ & + \frac{p}{2} \ell^{3} \left[M_{w\eta}^{'} \dot{q} \dot{q} (\eta - 1) \right] \\ & + \frac{p}{2} \ell^{3} \left[M_{w\eta}^{'} \dot{q} \dot{q} (\eta - 1) \right] \\ & + \frac{p}{2} \ell^{3} \left[M_{w\eta}^{'} \dot{q} \dot{q} (\eta - 1) \right] \\ & + \frac{p}{2} \ell^{3} \left[M_{w\eta}^{'} \dot{q} \dot{q} (\eta - 1) \right] \\ & + \frac{p}{2} \ell^{3} \left[M_{w\eta}^{'} \dot{q} \dot{q} (\eta - 1) \right] \\ & + \frac{p}{2} \ell^{3} \left[M_{w\eta}^{'} \dot{q} \dot{q} (\eta - 1) \right] \\ & + \frac{p}{2} \ell^{3} \left[M_{w\eta}^{'} \dot{q} \dot{q} (\eta - 1) \right] \\ & + \frac{p}{2} \ell^{3} \left[M_{w\eta}^{'} \dot{q} (\eta - 1) \right] \\ & + \frac{p}{2} \ell^{3} \left[M_{w\eta}^{'} \dot{q} (\eta - 1) \right] \\ & + \frac{p}{2} \ell^{3} \left[M_{w\eta}^{'} \dot{q} (\eta - 1) \right] \\ & + \frac{p}{2} \ell^{3} \left[M_{w\eta}^{'} \dot{q} (\eta - 1) \right] \\ & + \frac{p}{2} \ell^{3} \left[M_{w\eta}^{'} \dot{q} (\eta - 1) \right] \\ & + \frac{p}{2} \ell^{3} \left[M_{w\eta}^{'} \dot{q} (\eta - 1) \right] \\ & + \frac{p}{2} \ell^{3} \left[M_{w\eta}^{'} \dot{q} (\eta - 1) \right] \\ & + \frac{p}{2} \ell^{3} \left[M_{w\eta}^{'} \dot{q} (\eta - 1) \right] \\ & + \frac{p}{2} \ell^{3} \left[M_{w\eta}^{'} \dot{q} (\eta - 1) \right] \\ & + \frac$$

YAWING MOMENT

$$\begin{split} & I_{x} \dot{r} + (I_{y} - I_{x}) pq - (\dot{q} + rp) I_{yx} + (q^{2} - p^{2}) I_{xy} + (rq - \dot{p}) I_{zx} \\ & + m \left[x_{G} (\dot{v} - wp + ur) - y_{G} (\dot{u} - vr + wq) \right]_{x}^{2} \\ & + \frac{o}{2} t^{6} \left[N_{x} \dot{r} \dot{r} + N_{p} \dot{p} + N_{pq} \dot{p} q + N_{qr} \dot{q} r + N_{r|r|} \dot{r} \dot{r} \dot{r} \right] \right] \\ & + \frac{o}{2} t^{6} \left[N_{y} \dot{v} \dot{v} + N_{wr} \dot{w} r + N_{wp} \dot{w} p + N_{vq} \dot{v} q \right] \\ & + \frac{o}{2} t^{6} \left[N_{p} \dot{u} p + N_{r} \dot{u} r + N_{|r|} \dot{s} r' \dot{u} \dot{r} \dot{s} r + N_{|v|} \dot{r}' \dot{v} \dot{r} \dot{v} + w^{2} \right]_{x}^{\frac{1}{2}} \right] \\ & + \frac{o}{2} t^{3} \left[N_{y} \dot{u}^{2} + N_{v} \dot{u} v + N_{v|v|} \dot{v} \dot{v} \dot{v} \dot{v} \dot{v} + w^{2} \right]_{x}^{\frac{1}{2}} \right] \\ & + \frac{o}{2} t^{3} \left[N_{yw} \dot{v} \dot{v} w + N_{\delta r} \dot{u}^{2} \dot{s} r \right] \\ & + \left(x_{G} \dot{w} - x_{B} \dot{B} \right) \cos \theta \sin \theta + \left(y_{G} \dot{w} - y_{B} \dot{B} \right) \sin \theta' \\ & + \frac{o}{2} t^{4} N_{r} \dot{\eta}' \dot{u} r (\eta - 1) \\ & + \frac{o}{2} t^{3} \left[N_{v} \dot{\eta}' \dot{u} v + N_{v|v|} \dot{\eta}' \dot{v} \dot{v} \dot{v}^{2} + w^{3} \right]_{x}^{\frac{1}{2}} + N_{\delta r} \dot{\eta}' \dot{s}_{r}^{2} \dot{s}_{r}^{2} \right] (\eta - 1) \end{split}$$

A.3 AXIS TRAISFORMATIONS [2]

- 1) A transformation of an axes system takes a quantity described in one frame of reference and transforms it into another frame of reference such that if we measured the same quantity in the second frame of reference the transformed quantity and the measured quantity would be identical.
- Transforms between frames are needed in the study of the motions of ocean vehicles because the equations of motion for such a vehicle are most easily derived in the inertial frame attached to the earth (x_0, y_0, z_0) frame, while the forces acting on the vehicle are most easily evaluated in the frame attached to the vehicle (x, y, z). Hence, we ultimately desire to transform the equations of motion from the inertial frame into the non-inertial frame fixed in the vehicle.
- 3) If V_0 is some vector measure in the x_0 , y_0 , z_0 frame and V some vector measured in the x_0 , y_0 , z_0 frame which is only changed in orientation then:

 $\tilde{V}=T$ (φ , φ , ω) \tilde{V}_0 where T (ψ , φ , ϕ) = the transform. Where

 $\cos\theta \sin\theta$ $-\sin\theta$ $\cos\phi \cos\phi + \sin\phi \sin\theta \sin\phi$ $\sin\phi \cos\theta$ $-\sin\phi \cos\phi + \cos\phi \sin\theta \sin\phi$ $\cos\phi \cos\theta$

4) If V_0 and V are the same vectors as in (3) above, then: $\tilde{V}_{0} = T^{-1} (\phi, \phi, \phi) \tilde{V}$

Where

$$T^{-1}(\phi,\theta,\phi)=$$

CCS# COS# -sin≠ cosø + sinø sin∂ cos¢ cosø cosø + sinø sinø sinø cos# sin# sine cosa

sino sino + coso cos sino -sino cos+ + coso sind sine COS & COS A

-sing

APPENDIX B

B.1 LIST OF VARIABLES

VARIABLE	MEANING
A	Six by six matrix containing coefficients of UDT, VDT, WDT, PDT, QDT, RDT.
AA	Six by six matrix set equal to matrix A perfore each call to FUNC. The values of AA are lost in the matrix reduction performed by LEQTIF.
A1 ,A2	Limits used for selecting the proper propeller thrust.
AI,BI,CI	Set of constants representing the propeller thrust in the X-equation.
8	Ship's buoyancy.
BORATE	Average bowplane rate.
BOWNAX	Maximum ordered bowplane deflection.
COURSE	New course for the snip.
DECRIT	Value of depth error when dive planes are returned to zero deflection.
DELI	Calculated deflection of the bomplane.
DEL3	Calculated defrection of the stern plane.

DEL4	Calculated deflection of the rudder.
DELB	Actual bowplane deflection at time t.
DELBO	Actual bowplane deflection (units changed for output).
DELGM	Amount the original GM is to be changed.
DELR	Actual rudder deflection at time t.
DELRO	Actual rudder deflection (units changed for output).
DELS	Actual stern plane deflection at time t.
DELSO	Actual sterm plane deflection (units changed for output).
DELT	Time increment used in iteration.
OIFF	Difference between present depth and ordered depth.
ξ	Six by one matrix containing solution to right hand side of equations of motion.
ICNT	Counter used to count the number of iterations
ID	Forty-character alphanumeric heading.
LNDEX	If greater than zero, read new submarine coefficients. If less than or equal to zero, run same submarine for new initial

conditions.

IX, IY, IZ, IXY, IXZ, IYZ

Moments of inertia.

KCOEFF

K - equation coefficients:

1

Ship's overall length.

LEQTIF

Matrix reduction subroutine from IMSLIB [3]

н

Ship's mass.

MAXANG

Maximum ordered dive/ascent angle.

MCOEFF

M - equation coefficients.

NCOEFF

N - equation coefficients.

NODIFF

Acceptable error range around ordered depth.

NOP ICH

Acceptable error range around zero pitch

angle.

JOEPTH

Ordered depth.

OHCRS

Acceptable error range around ordered

course.

P.Q.R

Angular velocity about the x, y, and z

axes respectively.

POT, QOT, ROT

Angular acceleration about the x, y, and z

axes respectively.

POTO, GOTO, ROTO

Angular acceleration about the x, y, and z

axes, respectively (with units changed for output).

PHI

Angle of roll.

PHIO

Angle of roll (with units changed for

output).

PO,QO,RO

Angular velocity about the x, y, and z axes respectively (with units changed for output).

PSI

Angle of yaw.

PS10

Angle of yaw (with units changed for

output).

RHO

Sea water density.

RRATE

Average rudder rate.

RUDAMT

Maximum ordered rudder deflection.

STERAT

Average stern plane rate.

STERMX

Maximum ordered stern plane deflection.

STOW

Storage array for half of output data.

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Present time.

11 118

Time lag signais.

THETA

Angle of pitch.

57 THETAO Angle of pitch (with units changed for output). TLAGB Time lag for bowplane control system. TLAGR Time lag for the rudder control system. TLAGS Time lag for stern plane control system. W.V,U Forward, lateral, and vertical velocities respectively. TOW. TOY. TOU Forward, lateral, and vertical accelerations respectively (with units changed for output). UO. Initial forward velocity. OW. 0V. 00U Forward, lateral, and vertical velocities respectively (with units changed for output). W) Ship's weight. Coordinate labels of the fixed (xo, yo, X.Y.Z z_n) coordinate system.

18.Y3.4B The x, y, z position of the center of buoyancy.

XCOEFF X - equation coefficients

Velocities in the fixed coordinate system XDT.YUT.ZCT along the xo, yo, zo thes respectively.

The x, y, z position of the center of XG,YG,ZG

gravity.

YCOEFF

Y - equation coefficients

ZCOEFF

Z - equation coefficients

CUEFFICIENTS, ACCELERATIONS, VELOCITIES AND WRITE OUTPUT. CALCULATE LINEAR D.E. READ DATA & INITIAL CONDITIONS & INITIAL VALUES. INITIALIZE & NON-DIMENSIONALIZE. MAIN PROGRAM

MEAL *B XCOEFF(16), YCOEFF(22), ZCOEFF(22), KCOEFF(17), MCOEFF(23), NCOEFF(22), AA(6,6), E(6), A1(3), B1(3), C1(3), WKAREA(6,6) MPLICIT REAL*8(A-H), REAL*8(L-L)

REAL® K1,K2,K3,K4,K5,Kb,K7,KB,K9,K10 KLAL® 1X,1Y,1Z,1XY,1XZ,1YZ

KEAL *8 A(6.6),STON(600,11)

CUMPLIN / UNE/ K3, K4, K5, Kb, K7, KB, I3, I4, I7, IB, I9, I10, ILAGS, STERAT, STE KEAL 10(40)

CUMPEN / 1WU/ K1, K2, T1, T2, T13, T14, T15, T16, TLAGB, BORATE, BOMMAX, T, CHE ž

CUMPION / IHREE/ K9, KIU, 15, 16, T11, T12, T17, T18, ILAGR, RRATE, RUDAMI, COU

10EFF.WCOEFF.L.M.P.RHO.WT.B.XG.YG.ZG.IZ.IX.IY.IXZ.IXY.IYZ,RDT.QDT.P 20T.WDT.VDT.UDT.XB.YB.ZB.AI.AZ.AA.WKAREA COMMUN /FIVE/ THETA.Q.DELS.DELB.DELT.PSI.R.DELR COMMUN /FOUR/ U.V.W.UO.PHI.AI.BI.CI.XCOEFF.YCOEFF.ZCOEFF.KCOEFF.MC

READ NON-DIMENSIONAL COEFFICIENTS

COMPLIN /SIX/ DIFF, ADIFF, LDT, ATHETA, MAXANG, NOPICH, DCRIT

READ(5.16,ENU-999) INDEX INCE X=0

REAU(5,10,END-999) (XCOEFF(1),1-1,16) (YCOEFF(1),1-1,22) 1F (INDEX) 2,2,3 READ(5,10)

(11.1-1.((22'1-1') ZCOEFF(11) KCOEFF(1) KEAD(5.10) KLAD(5.10)

MCOEFF(1),1-1,23) MCDEFF(1),1-1,22 READ(5.10) KEAD(5,10)

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READ INITIAL CONDITIONS --- DEPTH, SPEED, ANGLES, ETC.
                                                                                                                                                                                                                                                                                                                                                                                                                                 READ SENSITIVITY PARAMETERS FOR COURSE, DEPTH & PITCH
                                                                       READ SHIP CHARACTERISTICS --- MASS, LENGTH, ETC.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        READ(5.18) TLAGR, COURSE, RRATE, RUMMT, DELT
                                                                                                                                                                                                       READ CONSTANTS FOR SHIP CONTROL SURFACES
                                                                                                                                                                                                                                                                                                                                                                                                                                                              READ(5,11) NODIFF, NOPICH, UNCRS, DCRIT
                                                                                                                                                                                                                                                                                                                            (10(1),1-1,40)
                                                                                                                                                                                                                                                                                                                                                                                                     DELS, DELB, DELR, DELCM, Z
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          READ COURSE CHANGE INFORMATION
                                                                                                                                                                                                                                                                                                                                                       READ(5,15) U.V.M.UOT.VUT.WDT
READ(5,15) P.Q.R.PUT.QUT.RDT
READ(5,12) THETA.PHI.PSI
READ(5,18) DELS.DELB.DELR.DEI
1xY, 1x2, 1Y2
WI, B
                                                                                                                                                                                                                                     READ(5,13) K1,K2
READ(5,11) K5,K6,K7,KB
READ(5,11) K9,K10
                                                                                                                                  M.L.RHU
IX, IY, 12
                                                                                                                   XB.YB.ZB
                                                                                                                                                                                                                                                                                                                           KEAD(5,14,END-999)
  KEAU(5.12)
REAU(5.12)
REAU(5.12)
REAU(5.12)
REAU(5.12)
REAU(5.12)
KEAD(5,10)
KEAU(5,10)
READ(5,10)
READ(5,13)
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42 FORMAT(20X, 'BASE SPEED =', F3.9, (KTS)', 10X, 'STARTING DEPTH =', F5.10', (FT)', 9X, 'STARTING COURSE = 000 (DEG)', //, 20X, 'DELTA T =', F3.12', (SEC)', (F3)', 0RDERED COURSE = 2', F4.0', (DEG)', //, 20X, 'RUDDER RATE =', F4.1', (DEG/SEC)', 4X, 'BOW P 4LANE RATE =', F4.1', (DEG/SEC)', 7X, 'BOW P LANE RATE =', F4.1', (DEG/SEC)', 7X, 'WAX BOW P LANE ANGLE ALLOWED =', F4.1', (DEG)', //, 20X, 'WAX STERN PLANE ANGLE ALLOWED =', F4.1', (DEG)', //, 20X, 'WAX STERN PLANE ANGLE ALLOWED =', F4.1', (DEG)', 6X, 'WAX DIVE ANGLE ALLOWED =', F4.1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              49 FURBAT (IH) 39X, ""./.40X," ".,40A)," ".,40A)," ".,/.40X,"",49X,"",49X,"" (/./.40X,"",49X,""),40X,"" (/./.40X,""),40X,"",40X,"",40X,"",49X,"")
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            51 FORMAT(5x, T., 11x, x, 10x, Y, 10x, Z, 10x, U', 10x, Y, 10x, W', 9x, 100T', 8x, VOT', 8x, WOT', 7x, OELS', 7x, OELS')
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    FORMAT(3X, '(SEC)', 7X, '(FI)', 7X, '(FI)', 7X, '(FI)', 7X, '(KTS)', 6X, '(KT
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 MRITE (6.42)U.Z, DELT, DEEPTH, COURSE, RRATE, BORATE, STERAT, RUDAMT, BOMMA
                                                                                                                                                                   READ(5,19)BORATE, BOMMAX, STERAT, STERMX, MAXANG, OUEPTH, TLAGB, TLAGS
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          (10(1),1-1,40)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  HRITE HEADING AND INPUTS
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             IX, STERMY, HAXANG
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  FURMAT (8010.4)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              FORMAT (5010.4)
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                                                                                                                                                                                                                                                                                                               FORMT (4010.4
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                                                                                                                                                                                                                                                   FORMAT (010.4)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           14 FORMT (40A1)
15 FURMAT (6010.
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READ DEPTH CHANGE INFORMATION

A(2,1)=0.0 A(2,2)=H-YCOEFF(6)

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15)'.6X,'(KTS)'.4X,'(KTS/SEC)'.2X,'(KTS/SEC)'.2X,'(KTS/SEC)'.3X,'(D
2EG)'.7X,'(UEG)')
                                                                                                                                                                                             IF CM IS BEING CHANGED CALCULATE NEW VERTICAL CENTER OF BUDYANCY
                                                                                                                                                                                                                                                                                                                                                                                                                                                                 CALCULATE COEFFICIENT VALUES FOR THE SIX LINEAR D.E.'S
                                                                                                                                                                                                                                                                     NON-DIMENSIONALIZE MASS AND NOMENTS OF INERTIA
                                                           INITIALIZE STORAGE MATRIX
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          A(1,1)=H-XCOEFF(4)
A(1,2)=0.0
A(1,3)=0.0
A(1,4)=0.0
A(1,5)=H*Z6
                                                                                                                                                                                                                                                                                                            H-H/(.5°RHO*(L**3))
                                                                                                                                                                                                                                                                                                                            DENDM- SORYDON (LOSS)
                                                                                             00 46 J-1,11
00 46 JJ-1,600
STOM(JJ,J)-0.001
CONTINUE
                                                                                                                                                                                                                                                                                                                                                                                                       IXY-IXY/LENDM
                                                                                                                                                                                                                                                                                                                                                                                                                       172-172/DENOM
                                                                                                                                                                                                                                                                                                                                                                                                                                       HON30/7X1-7X8
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    A(1,6)--M*YG
                                                                                                                                                                                                                                                                                                                                                                                   17-11/DENOM
                                                                                                                                                                                                                                                                                                                                                  IX-IX/DENOM
                                                                                                                                                                                                                                                                                                                                                                   IY-IY/UENON
                                                                                                                                                                                                                                          M9 130-87-87
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A(2.4)=0.0
A(2.4)=-(W=ZG+YCOEFF(2)=L)
A(2.5)=0.0
A(3.2)=0.0
A(3.1)=0.0
A(3.2)=0.0
A(3.3)=W=ZG+F(5)=L
A(3.4)=W=ZG+F(5)=L
A(3.5)=-(W=ZG+F(5)=L)
A(3.5)=-(W=ZG+F(5)=L)
A(3.5)=-(W=ZG+ZG)=L)=L
A(3.5)=-(W=ZG+ZG)=L)=L
A(3.5)=-(W=ZG+ZG)=L)=L
A(3.5)=-(W=ZG+ZG)=L)=L
A(3.5)=-(W=ZG+ZG)=L)=L
A(3.5)=-(W=ZG+ZG)=L)=L
A(3.5)=-(W=ZG+ZG+ZG)=L
A(3.5)=-(W=ZG+ZG+ZG
```

```
CUNVERT ANGLES IN DEGREES TO RADIANS AND KNOTS TO FT/SEC FOR INTERNAL USE.
                                                                                                                                                             UDT-UDT-1.6889
VDT-YDT-1.6889
WDT-WDT-1.6889
PHI-PHI/57.2958
                                                                                                   UO-UO*1.6889
U-U*1.6889
V-V*1.6889
APH1=0.
CRS2=100.
                            CHECK-0.
                                                                                      n-0n
```

ATHETA-0.

ADIFF-0.

X=0.001 Y=0.001 XUI=0.

YUI-U.

ZuT=0.

111-1.

110-1.

18-1 19-1

[5•]. [6•].

```
THE TA-THE TA/57.2958
PSI*PSI/57.2958
COURSE-COURSE/57.2958
RRATE-RRATE/57.2958
RUGAMI-RUMAMI/57.2958
BUMMAX-BUMATE/57.2958
STERAT-STERAT/57.2958
STERAT-STERAT/57.2958
GURCKS-ONCRS/57.2958
UNCRS-ONCRS/57.2958
TO TE TERAT/57.2958
TO TERAT/57.2958
```

EACH CALLING TO 'FUNC' WILL DESTROY 'AA' MATRIX DURING GAUSSIAM REDUCTION. TO 'A' MATRIX. AS EACH ITERATION BEGINS, INITIALIZE 'AA' MATRIX EQUAL

C AS EACH ITERATION C EACH CALLING TO 'F C 30 DO 53 K=1,6 DO 53 JJ=1,6 AA(K,JJ)=A(K,JJ) 53 CONTINUE CALL 'FUNC' SUBROUTINE AND CALCULATE ACCELERATIONS AT TIME T + DELTA T.

CALL FUNC

UPDATE ANGLES AND VELOCITIES

PHI=PHI+(DELT*P)+((DELT**2)/2)*PDT
THETA=THETA+(DELT*Q)+((DELT**2)/2)*QOT
PSI=PSI+(UELT*R)+((DELT**2)/2)*RDI
U=U+UELT*UUT
V=V+UELT*VUT
W=W+UELT*WUT
P=P+UELT*WUT
Q=Q+UELT*QUT

```
CALL SUBMOUTINES TO ALJUST RUDDER AND PLANES AS NECESSARY TO ACHIEVE
                                                                              XUT- ((U*(UCOS(THETA)*UCUS(PSI))+V*(-USIN(PSI)*UCOS(PHI)+USIN(P
1HI)*USIN(THETA)*UCOS(PSI))+W*(USIN(PHI)*USIN(PSI)+UCUS(PHI)*UCOS(P
2SI)*USIN(THETA)))*UKLT)
                                                                                                                                                                                                                       ZDI- ((U-(-DSIN(THEIA))+V-(DSIN(PHI)+DCOS(THEIA))+W-(DCOS(PHI)+DCDS(THEIA)))+W-(DCOS(PHI)+DCDS(THEIA))
                                                                                                                                                        (U.(U.COS(THETA).USIN(PSI))+V*(UCOS(PHI)*DCOS(PSI)+USIN(PH
                                                                                                                                                                            1) -USIN( THE TA) -DS IN(PSI )) +W* (-USIN(PHI) *DCOS(PSI) +DCOS(PHI) *DSIN(T
                                                                                                                                                                                                                                                                                                  CALCULATE POSITION OF SUBMARINE (X,Y,Z) AT TIME T + DELTA T.
                                        CALCULATE VELOCITY OF SUBMARINE IN FIXED COORDINATE SYSTEM
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       IF ((AUIFF.LT. DCRIT). AND. (ATHETA.GT. HOPITCH)) CALL STERN
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     IF ((CRSZ.GI.ONCRS).UR. (UELK.NE.O.)) CALL RUDDER
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 CKS2*UABS(PI-CRS1+PSI)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              CRS2*LABS (COURSE-PSI)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             IF (AUIFF. GT. MULLEF) CALL DEPTH
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       IF (ADIFF. GT. DCRIT) CALL STERN
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           UKDERED COURSE AND DEPTH
                                                                                                                                                                                                          ZHETA) +USIM(PSI))) +DELT)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                           ATHE TA-DABS (THE TA)
                                                                                                                                                                                                                                                                                                                                                                                                                                                       ADIFF-DABS(DIFF)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      IF (CRS).61.0. \
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          CRS 1-COURSE -P1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     APSI-UABS(PSI)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    IF (CRS1.LE.O.)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            APHI-LABS (PHI
                                                                                                                                                                                                                                                                                                                                                                                                                               D1FF-2-00EPTH
                                                                                                                                                                                                                                                                                                                                                                               Y-Y+UEL I-YUI
                                                                                                                                                                                                                                                                                                                                                                                                      192-1199-7-2
                                                                                                                                                                                                                                                                                                                                                        X-X+DELT*XDT
K-K+UKLT-RDF
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  PI-3, 14159
                                                                                                                                                                     YU].
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     ~
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CONVEKT ANGLES IN RADIANS TO DECREES AND FT/SEC TO KNOTS FOR OUTPUT
                                                                                                                                                                                                                                          THE TAO- TIE TA-57, 2958
                                  | POTO=POT=57.2958
QUTO=QOT=57.2958
ROTO=ROT=57.2958
DELRO=DELR=57.2958
                                                                                                     JK15U-DE15*57.2958
                                                                                                                       M. BO-W. LB . 57, 2958
                                                                                                                                                                                                         PS10-PS1*57,2958
PH10-PH1*57,2958
                                                                                                                                       PHIU-PHI*57.2958
                                                                                                                                                                                                                                                            UDTO-UDT/1,6889
VDTO-VDT/1,6889
WCTO-WBT/1,6889
                                                                                                                                                                                                                                                                                                                              QC=Q*51,2958
BO+R*57,2958
                                                                                                                                                                                                                                                                                                              PO-Pn57, 2958
                                                                                                                                                        UCU-0/1.6889
                                                                                                                                                                         VU-V/1.6089
                                                                                                                                                                                           #D=U/1.6889
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STORE VALUES THAT CANNOT BE WRITTEN NOW IN MATRIX "STOM" FOR OUTPUT LATER WITH A NEW HEADING.

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510M(3,1)+1 519M(3,2)+PH10 510M(3,3)+1HETA0 510M(3,4)+PS10 510M(3,5)+P0 510M(3,5)+P0 510M(3,9)+P010 510M(3,10)+R010 510M(3,10)+R010 510M(3,10)+R010

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4/ FORMAT (3X, (SEC)', 6X, '(DEG)', 6X, '(DEG)', 6X, '(DEG)', 4X, '(DEG/SEC)'
1,2X, '(DEG/SEC)', 2X, '(DEG/SEC) (DEG/SEC2) (DEG/SEC2) (DEG/SEC2)', 4X
2, '(DEG)')
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               44 FURMAT(5x, T', 11x, 'PHI', 6x, 'THETA', 6x, 'PSI', 10x, 'P', 10x, 'Q', 10x, 'R
*', 9x, 'PUI', 8x, 'QUI', 8x, 'KDI', 7x, 'UELR')
WRITE(6,47)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             39 WRITE(6,48) (10(1),1-1,40)
48 FORMAT(1H1,39x,"...,49x,"...,40x,"...,40x,"...,49x,"...
1-1,40x,"-1,40x,"-1,40x,"-1,40x,"...,40A1,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40x,"...,40
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           END CALCULATIONS WHEN ORDERED COURSE AND DEPTH IS REACHED
IF((CRS2.LE.ONCRS).AND.(ADIFF.LT.NCDIFF).AND.(ATHETA.LE.NOPICH).AN
10.(APHI.LE.1.0)) GO TO 39
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     WRITE HEW HEADING FOR OUTPUT THAT HAS BEEN STORED IN MATRIX 'STOM'
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       END CALCULATIONS WHEN "ICNT" NUMBER OF ITERATIONS ARE COMPLETE.
MRITE (6,50)T,X,Y,Z,U00,V0,WU,UUTU,VUTO,WUTO,DELSO,DELBO 50 FURMAT(3(1X,D10.3),D11.4.8(1XD10.3),/)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            CHECK TO SEE IF NEW DATA IS MAITING FOR ANOTHER RUN.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        MRITE(6,43)((STOM(J,1),1=1,11),J=1,1CNT)
43 FORMAT(11(1x,010.3),/)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           IF (1CMT.GE.600) GO TO 39
                                                                                                                                                                                                                                                                                                    TIME INCREMENT ALGORITIM
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 ICMT-ICMT+1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   2 2 3
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             2) 1-T+UELT
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              ----
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      ں ں
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SUBHOUTINE FUNC CALCULATES THE RIGHT HAND STDE OF THE SIX NON-LINEAR
                                                                                                                                                  CUMPUN /FOUR/ U.V.W.UO,PHI.AI,BI.CI.XCOEFF.YCOEFF.ZCOEFF.KCOEFF,MC
10EFF.NCGEFF.L.M.F.NBG.WI.B.XG.YG.ZG.IZ,IX,IX,IXZ,IXY,IYZ.RDI.QDI.P
2UI.WOI.VUI.UOI.XB.YB.ZB.AI.AZ,AA.WKAREA
                                                IMPLICIT REAL*8(A-H), REAL*8(L-Z)
REAL*8 XCUEFF (16), YCOEFF (22), JCOEFF (22), KCOEFF (17), MCOEFF (23), NCOE
IFF (22), AA(6,6), E(6), AI(3), BI(3), CI(3), WKAREA(6,6)
REAL*8 IX, IY, IZ, IXY, IXZ, IYZ
                                                                                                                                                                                                                                        COMPON /FIVE/ THETA, Q, DELS, DELB, DELT, PSI, R, DELR
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              TEST FOR APPROPRIATE THRUST/DRAG COEFFICTION
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                IF(ETA.LE.A1) GO TO 10
IF((ETA.GT.A1).AMD.(ETA.LE.A2)) GO TO 11
                                                                                                                                                                                                                                                                                                                                                                                                                            CALCULATE MAGNITUDE OF VECTOR VELOCITY
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    81GU=D$URT(U**2+V**2+W**2)
                                                                                                                                                                                                                                                                                                                        DIFFERENTIAL EQUATIONS.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        IF(ETA.GT.A2) GO TO 12
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             W-USQRT (V**2+W**2)
SUBMOUTINE FUNC
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      THE TAN-THE TA
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              E TA-U0/BIGU
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        AII-AI(2)
BII-BI(2)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   \(\bar{1}\)
                                                                                                                                                                                                                                                                                                                                                                          LTA-0.001
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            811-81(1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       (1)10-1110
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 3 2 3
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  PHIK-PHI
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   2
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A11-A1(3) C11-C1(2) 3 5 40 E)[9-1]8 ()11-11) 2

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RIGHT-HAND-SIDE OF LINEAR D.E.'S FOR UDT, VOT, NDT, POT, QOT, AND ROT. 5{DELR*U)**2}**COEFF(16)*((DELS*U)**2)))-((2./(PHD*(L**3)))*(WT-B)* 1(5)*V*R+XCUEFF(6)*W*Q)+((1./L)*(XCOEFF(7)*(U**2)+XCOEFF(8)*(V**2)+ 40 E(1)=(L*(XCOEFF(1)*(Q**2)+XCOEFF(2)*(R**2)+XCOEFF(3)*R*P))+(XCOEFF 4((1./L)*(£TA-1.)*(XCÓEFF(13)*(V**2)*XCJEFF(14)*(W**2)*XCOEFF(15)*(2XCOEFF(9)*(W**2)+AII*(U**2)+BII*U*U0+CII*(10**2)))+((1./L)*(U**2) 3(XCOEFF(10)*(DELR**2)*XCOEFF(11)*(DELS**2)*XCOEFF(12)*(DELB**2))) 605IN(THETAR))-(H*(W*Q-V*R-AU*((Q**2)+(R**2))+YG*P*Q+ZG*P*R)

VV-V IF (VV. Eq. 0.001) VV-0.10-15

40EFF(16)*V*UABS(VW)*VCOEFF(17)*V*W*YCOEFF(18)*(U*"2)*DELR)}+((2/(R E(2)*L*(YCOEFF(3)*P*DABS(P)+YCOEFF(4)*P*U+YCOEFF(5)*Q*R)+(YCOEFF(7 20EFF(12)*U*DABS(R)*DELR+VCOEFF(13)*(V/DABS(VV))*DABS(VW)*DABS(R)*Y XOEFF(19)*U*R*(ETÄ-1))*((1/L)*(*COEFF(14)*(U**2)*YCOEFF(15)*U*V*YC 5H)*[.**3])*(NI-B)*DCOS(THETAR)*DCOS(PHIR))*(((1/L)*(ETA-1))*(YCOEFF 6(20)*U*V+YCOEFF(21)*V*DABS(VW)+YCOEFF(22)*DELR*(U**2)))-(H*(U*R-W* 7P-YG+(Ran2+P**2)+1G+U*R+XG*(PP))

IN. EQ. 9. 001) WA-0. 10-15

20) = (H/UMBS(WW)) * BABS(VW) * DABS(Q) + 2COEFF(11) * U*Q*(ETÄ-1)+((1/L)*(2C 30EFF(12)*(U**2)*2C0EFF(13)*U*W+2C0EFF(14)*W*DABS(VW)*2C0EFF(15)*U* fUABS(W)+2COLFF(16)+UABS(W+W)+2COEFF(17)+(Y**2)+2COEFF(18)+(U**2)* E(3)=(L=(2COEFF(2)*P**2+2COEFF(3)*(K**2)+2COEFF(4)*R*P))+2COEFF(6) |•V*R+ZCUEFF(7)*V*P+ZCOEFF(8)*U*Q+ZCOEFF(9)*U*DABS(Q)*DELS+ZCOEFF(

5UELS+2CORFF(19)*(U**2)*DELB))* ((1/L)*(ETA-1))*(ZCOEFF(20)*U*W+ZCO 6LFF(21)*W*DABS(W)+2COEFF(22)*DELS*(U**2))*((2/(WW*L**3))*(WI-B)* /UCUS(TIR.TAR)*DCOS(PHIR))-(M*(V*P-U*Q-ZG*((P**2)+(Q**2))+XG*R*P+YG* SK (U)

4))+((2/(WW-L++5))+((YG-WT-YB-B)+DCOS(THE TAR)+DCOS(PHTR)-(ZG+WT-ZB 5+B)+DCOS(THE TAR)+DSIN(PHTR))-((TZ-TY)+Q+R)+(TXZ+Q+P)-((R++2-Q++2) IF (b) *U*P*KCOEFF (7) *U*R*KCOEFF (9) *V*Q*KCOEFF (10) *W*P*KCOEFF (11) *W*R 2))+{(1/L**2)*(KCOEFF(12)*(U**2)+KCOEFF(13)*V*U+KCOEFF(14)*V*DABS(V 34)+KCOEFF(15)*V*W+KCOEFF(16)*(U**2)*DELR+KCOEFF(17)*(U**2)*(ETA-1) E(4)=KCOEFF(3)=Q=R+KCOEFF(4)=P=Q+KCOEFF(5)=P=DABS(P)+((1/L)=(KCOEF 6-142)-1xyepeR-((M*(1/L**2))*(YG*(V*P-U*Q)-ZG*(U*R-W*P))

7*(ETA-1)*(HCDEFF(21)*U*W+MCDEFF(22)*W*(MBS(VW)+HCDEFF(23)*DELS*(II* 518)*(U**2)*DELS+MCDEFF(19)*(U**2)*DELB))*((2/(RIM*L**5))*((XG*WT-X 68-8)-DCOS(THETAR)-DCOS(PHÍR)-(26-WT-28-8)-DSIN(THETAR)))+((1/L-+2) N-2)))-(IY-IX)*P*Q+IYZ*R*P-IXY*((Q**2)-(P**2))-IXZ*R*Q-(H*(1/L**2)* E(5)+(MCOEFF(2)+P++2+MCOEFF(3)+(K++2)+MCOEFF(4)+R+P+MCOEFF(5)+Q+DA 135(4))+((1/L)*(MCOEFF(7)*V*R*MLOEFF(8)*V*P*NCOEFF(9)*U*Q*MCOEFF(10 31/L**2)*(MCOKFF(12)*(U**2)*MCOEFF(13)*U*W+MCOEFF(14)*W*DABS(VM)*MC 40EFF(15)*U*UAB: (W)+MCDEFF(16)*DABS(W*VW)+MCOEFF(17)*(V**2)+MCOEFF(2)*U*DABS(Q)*DELS+MCOEFF(11)*DABS(VW)*Q+MCOEFF(20)*U*Q*(ETA-1)))+(9(XG*(U*R-W*P)-YG*(W*Q-V*R)))

1(7) *W*R+NCOEFF(8) *W*P+NCUEFF(9) *V*Q+NCOEFF(10) *U*P+NCOEFF(11) *U*R*ZNCOEFF(12) *U*DABS(K) *DELR+NCOEFF(13) *DABS(VN)*R) +((1/L**Z)*(NCOEF 5DSIN(PHIR)+(YG*WI-YB*B)*DSIN(THETAR)))+((1./L)*(ETA-1.)*NCOEFF(19) 6*U*R)+((1./L*2)*(ETA-1.)*(NCOEFF(20)*U*Y+NCOEFF(21)*Y*DABS(VW)+NC 3F (14)+U++2+NCOEFF (15)+U+V+NCOEFF (16)+V+DABS (VW)+NCOEFF (17)+W+NCO 4EFF(18)*(U**2)*DELR))*((2./(NHO*L**5))*((XG*NT-XB*B)*DCOS(THETAR)* 7UEFF(22)*UKLR*U**2))-((IY-IX)*P*Q)+(IYZ*P*K)-(IXY*(Q**2-P**2))-(IX E(b)=ncolff(3)=p=tj+ncolff(4)=q=R+ncolff(5)=R=dabs(R)+(1/L)=(ncolff 82*P*R)-(M*(1./L**2)*(XG*(U*K-W*P)-YG*(W*Q-V*R)))

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THIS CALL PERFORMS THE GAUSSIAN REDUCTION OF THE 'AA' MATRIX. LEQTIF IS A LIBRARY FUNCTION IN SYSS.INSLIB.

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CALL LEQTIF (AA.1.b.6.E.3.WKARLA.1ER)
RDT=E(6)
QDT=E(5)
PDT=E(4)
WDT=E(2)
UDT=E(2)
WDT=E(2)
END
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REAL*B K1, K2, K3, K4, K5, K6, K7, KB, K9, K10
COMPLON / THREE/ K9, K10, T5, T6, T11, T12, T17, T18, YLAGR, RRATE, RUDANT, COU
                                                                                                                                                                                                                                                                                                                                       PERFORM A TEST TO DECIDE WHICH WAY TO TURN. DCORS REPRESENTS
                                                                                                                                                                                                                                                                                                                                                                      THE DIFFERENCE BETWEEN THE PRESENT HEADING AND THE ORDERED
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         CALCULATED RUDDER DEFLECTION IS PROPURTIONAL TO THE ERRUR
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              WHEN THE MUDEL IS NEARLY ON COURSE THE RUDDER SHOULD BE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              BROUGHT ARIDSHIPS AND THE ANGLEAR VELOCITY SHOULD BE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    ENSURE TIME LAG HAS PASSED BEFORE RUDDER HOVES.
                                                                                                                                                                                 CUMPRON /FIVE/ THE TA, Q, DELS, DELB, DELT, PSI, R, DELR
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       IF(IEST.LE.O.) DCDRS-COURSE-PSI
IF(IEST.GT.O.) DCDRS--((PI-TEST)+PSI)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               1F (UABS (UCORS).1E.CLOSE) GO TO 18
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              SIGNAL AND THE ANGULAR VELOCITY.
                                                         IMPLICIT REAL®B(A-H), REAL®B(L-L)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            IF (ULL4.GT.0.) GO TO 1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               UEL 4-K9-UCORS+K1U*R
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     CLOSELY MONITORED.
SUBROUTINE KNUOER
                                                                                                                                                                                                                                                                                   UKL 1A-RRATE "UKLT
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    CLOSE .. 12 . TEST
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                TEST-COURSE-P1
                                                                                                                                                                                                                                                        PI-3,14159
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AS ERROR SIGNAL GETS SWALLER, RUDUER ANGLE CAN BE REDUCED.
                                                                                                                         ENSURE MAX. ORDERED RUDDER DEFLECTION IS NOT EXCEEDED.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                ENSURE MAX. ORDERED RUDDER DEFLECTION IS NOT EXCREDED.
                                                                                                                                                                                                                                                                                     ENSURE TIME LAG HAS PASSED BEFORE RUDDER MOYES.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        LHSURE TIME LAG HAS PASSED BEFORE RUXDER MOVES.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    ENSURE TIME LAG HAS PASSED BEFORE KURKER MOVES.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            10 IF (DABS (DELR), GE. RUGAMT) DELR -- RUDAMT
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              IF (UABS (DEL4). LT. DABS (DELR)) GO TO 6
DELR-DELR-DELTA
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         IF (DELTB.LT.DELTA) DELR-DELR-DELTB
IF (DELTB.GT.DELTA) DELR-DELR-DELTA
IF (T6.LE.TLAGR) GO TO 3
IF (DABS(DEL4).LT.DELR) GO TO 5
UELR-DELR+OELTA
                                                                                                                                                                                      14 IF (DELR.GE. RUDANT) DELR-RUDANT
                                                                                                                                                                                                                                                                                                                                                                                   IF(112.1E.1LAGR) GO TO 7
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     IF(T5.LE.TLAGR) GO TO 4
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              DELTB-DELR-DABS (DEL4)
                                                                                                                                                                                                                         3
2
3
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            323
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AS EKROR SIGNAL GETS SMALLER, RUDDER AMGLE CAN BE REDUCED.
                                                                                                                                                                                                                                                                                                                                                                                                                    ENSURE TIME LAG HAS PASSED BEFORE RUNDER MOVES.
                                                                                                                                                                                                                                                                    ENSURE TIME LAG HAS PASSED BEFORE RUDKER MOVES.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             IF ((ULLR.GT.0.). AND. (DCUPS.GL.0.)) GO TO 15
                                                                                                                                                                                                                                                                                                                                                               IF((DELR.LT.0.), AND. (DCORS.LE.O.)) GO TO 15
                                                                                                                                                            ALGURITIM FOR SMALL ERROR SIGNALS.
                                                                   UELTB-UABS(DELR)-UABS(UEL4)
IF(UELTB.LT.UELTA) DELR-DELRE
IF(DELTB.GT.UELTA) UELR-DELR+UELTA
                                                                                                                                                                                                                                                                                                                                                                                                                                                                             JF(117.LE.TLAGR) GO TO 13
WELR+WELR+DELTA
                                                                                                                                                                                                                                                                                                                               IF (118.LE.TLAGR) GO TO 9
IF(111.LE.TLAGR) GO TO 8
                                                                                                                                                                                                    IF(R.LI.O.) 60 TO 11
IF(R.GI.O.) 60 TO 12
                                                                                                                                                                                                                                                                                                                                                  UELR-UELK-DELTA
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                117-117-WLT
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            9 118-T18+DELT
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            66 01 09
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       50 70 14
                                                                                                                                                                                                                                           50 10 99
                                                                                                                                66 01 03
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          KLR-U.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                  12 TIB-0.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    <u>~</u>
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3 T6=T6+DLLT GD T0 99 4 T5=T5+DLLT GD T0 99 J T12=T12+DLLT GD T0 99 B T11=T11+DLLT 99 RETURN

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SUBKOUTINE DEPTH

IMPLICIT REAL*8(A-H), REAL*8(L-Z)

KEAL*8 K1,K2,K3,K4,K5,K6,K7,K8,K9,K10

COMMON /TWD/ K1,K2,T1,T2,T13,T14,T15,T16,TLAGB,BURATE,BOMMAX,T,CHE

ICK

COMMON /FIVE/ THETA,Q,DELS,DELB,DELT,PSI,R,DELR

CUMPON /SIX/ UTFF,ADIFF,20T,ATHETA,MAXAMG,NOPICH,DCRIT

CALCULATED DIVE PLANE ANGLE IS PROPURTIONAL TO DEPTH ERROR SIGNAL AND RATE OF CHANGE OF DEPTH.

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DEL 1-K1-DIFF+K2-LDT ADEL 1-DABS (DEL 1) UEL TA-BUKATE-DEL T DEL TB-UABS (DEL 8)-ADEL 1 IF THE EINOR SIGNAL IS SMALL GO TO 18 FOR FINER CONTROL.

IF (AUIFF.LT. DCRIT) GO TO 18
IF (DELI.LT.O.) GO TO 4

ENSURE TIME LAG HAS PASSED BEFORE PLANE MOVES.

12=0. 1F(11.LE.1LAGB) GO 10 89 IF MAX DIVE/ASCENT ANGLE IS EXCEEDED TAKE CORRECTIVE ACTION.

5 IF((ATHETA.GE.MAXANG).AND.(THETA.GE.O.)) GU TO 2
DELB-DELB+DELTA
IF(DELB.GT.ADEL1) GU TO 10

ENSURE MAX PLANE ANGLE IS NOT EXCEEDED.

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AS ERRUR SIGNAL GROWS SMALLER, THE PLANE ANGLE CAN BE REJUCED.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   IF MAX DIVE/ASCENT ANGLE IS EXCEEDED TAKE CORRECTIVE ACTION.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                IF MAX DIVE/ASCENT ANGLE IS EXCEEDED WRITE DIAGNOSTIC.
                                          IF MAX DIVE/ASCENT ANGLE IS EXCLEDED WRITE DIAGNOSTIC.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           IF ((ATHETA.GE.MAXANG). AND. (THETA.LE.O.)) GO TO 3
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          ENSURE TIME LAG HAS PASSED BEFORE PLANE MOVES.
                                                                                                                                                                                                                         ENSURE TIME LAG HAS PASSED BEFORE PLANE MOVES.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   ENSURE MAX PLANE ANGLE IS NOT EXCEEDED.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     B IF (DABS (DELB). GE. BUMMAX) DELB=-BOMMAX
                                                                                                                                                                                                                                                                                                                                                                                                           IF (DELTB.LE.DELTA) DELB-ADELI
IF (DELTB.GT.DELTA) DELB-DELBA
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                IF (UABS (DELB). GT. ADEL 1) GO TO 11
9 IF (DELB. GE. BOWMAX) DELB-BOWMAX
                                                                                                   LE (ATHETA. GE. MAXAMS) GO TO 6
                                                                                                                                                                                                                                                                                                            1f(116.LE.1LAGB) GO TO BB
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              IF(12.LE.1LAGB) GO TO 90
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            ULLB-ULLE-UKLTA
                                                                                                                                                          2 DELIB-DELB-DELTA
                                                                                                                                                                                                                                                                                           10 115-0.
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7 FURNAT(/,20X,'**** EXCEEDED MAX DIVE/ASCENT ANGLE AT TIME =',F10
                                                                                                                                                                  AS EKRUR SIGNAL GROWS SMALLER, THE PLANE ANGLE CAN BE REDUCED.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           50 70 13
                                                                                                                                                                                                                                                                                                                                                                                                                                                                      GO TO 14
GO TO 12
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          50 TO 12
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       RE TURN
                                                                                                                                                                                                                                                                                                                                                                                                                                                     RETURN
                                                                                                                                                                                                                                                                                                                                            "..... , 20X, ".... STANDARD FIXUP TAKEN *****
                                                                                                                                                                                                                                                                                                                                                                                                                                       IF ((201.LT.0.).AHD. (DIFF.GT.D.).AND. (DELB.EQ.0.))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              .. AND. (DIFF.LT.G.).AND. (DELB.LT.-4.)
                                                                                                                                                                                                                                                                                                                                                                                                                                                      (WELB. EQ. 0.)
DELB. LE. 4.)
UELB. NE. 0.)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          . AND. (DELB. GE. -4.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             DELB.NE.O.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          DELB.CT.4.
                                                                                ENSUME TIME LAG HAS PASSED BEFORE PLANE MOVES.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            . AMD. (
                                                                                                                                                                                                                                                                                                                                                                                                                                                                           . AMD.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             . MD. (
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               . AMD. (
                                                                                                                                                                                                                                                                                                                                                                                                                                                        . AMD. (
                                                                                                                                                                                                         JF (DELTB.LE.DELTA) DELB*-ADEL1
JF (DELTB.GT.DELTA) DELB*DELB*DELTA
                                                                                                                                                                                                                                                                                                                                                                                                      CONTROL FOR SMALL ERROR SIGNALS.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                         . AND. (UIFF.GT.O.).
. AND. (DIFF.LT.O.).
. AND. (UIFF.GT.O.).
. AND. (UIFF.GT.O.).
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                . AND. (UTFF.LT.O.)
                                                                                                                                                                                                                                                                                                                                                                                                                                                         (201.G1.0.). AND. (D1FF.LT.0.)
1F (ATHE TA. GE. MAXANG) GO TO 6
                                                                                                                                                                                                                                                                                DIAGMSTIC WRITE STATEMENT
                                                                                                                                       1F(115.LE.TLAGB) GO TO B7
                                    3 DELB-DELB+DELTA
                                                                                                                                                                                                                                                                                                                                                                                                                                                                              (201.61.0.)
(201.61.0.)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     IF ((ZDT.LT.O.)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      11 (DELB.LT.O.)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   (2DT.LT.O.)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   201.LT.U.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                201.61.0.
                                                                                                                                                                                                                                                                                                                     6 MRITE (6,7)T
                                                                                                                                                                                                                                                GU 10 92
                     20 33
20 43
                                                     6 22 33
                                                                                                                            11 116-0.
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90 12-12-DEL1

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ENSURE TIME LAG INS PASSED BEFORE PLANE MOVES.
                                                                                                                                                                                     ENSURE TIME LAG MAS PASSED BEFORE PLANE MOVES.
                                                                                                         23 IF((ULLB-DELTA) .LT.U.) GO TO 15
20 UELB-UELB-GELTA
                                                                                                                                                                                                                                                                                               21 IF((DELB+DELTA).GT.O.) GO TO 15
19 DELB+DELBA
                                                                                                                                                                                                                                 IF (T13.LE.TLAGB) GO 10 16
IF (CHECK.EQ.1.) GO TO 21
IF (DELB.LT.6.) GO TO 19
                                            15 (114.LE.TLACB) GO TO 17 11 (CHECK.EQ.2.) GO TO 23 15 (DELE.GT.-6.) GO TO 20 GO TO 91
                                                                                                                                                                                                                                                                                                                                                            60 To 31
                                                                                                                                                                                                                                                                                                                                                                                                          77 114-114+DELT
                                                                                                                                                                                                                                                                                                                                                                                                                                                                       116-116+UELT
                                                                                                                                                                                                                                                                                                                                                                                                                                        87 115-1115+DELT
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       11-111-0617
                                                                                                                                        GO TU 92
                                                                                                                                                                                                                                                                                                                                                                                                                          16 01 03
                                                                                                                                                                                                                                                                                                                               GU TU 92
                                                                                                                                                                                                                                                                                                                                                                                           GO 10 91
                                                                                                                                                                                                                                                                                                                                                                                                                                                         12 01 03
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       16 01 09
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       CO TC 91
                                                                                                                                                       CHECK+1.
                                                                                                                                                                                                                                                                                                                                             DELB-U.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                          3
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GD 10-91
1F(DELB.LT.-BOMMAX) DELB--BOMMAX
1F(DELB.GT COMMAX) DELB-BUMMAX
91 KETURN
END

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SUBROUTINE STERN
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KEAL*B KI, K2,K3,K4,K5,K6,K7,KB,K9,K10
CUMPLIN /UNE/ K3,K4,K5,K6,K7,KB,T3,T4,T7,TB,T9,T10,TLAGS,STERAT,STE
                                                                                                                                                                        COMPION /FIVE/ THE TA, Q, DELS, UKLB, DELT, PSI, R, BELR COMPION /SIX/ UTFF, ADIFF, 201, ATHETA, MAXANG, NOPICH, DCRIT
IMPLICIT REAL*8(A-H), REAL*8(L-Z)
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CALCULATED PLANE ANGEL IS PRUPORFIONAL TO DEPTH ERROR, RATE OF CHANGE OF DEPTH, PITCH ANGEL, AND RATE OF CHANGE OF PITCH.

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UEL3-K5-DIFF+K6-ZDT+K7-THETA+K8-Q
AULL3-DABS(DEL3)
DELTA-STERAT-DELT
DELTB-UABS(DELS)-AC-L3
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FOR SMALL DEPTH EKKUR AND LARGE PITCH ERROR GO TO 18

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IF ((ADIFF.LI.DCRII).AND. (ATHETA.GT.MOPICH)) GO TO 18 IF (UEL3.GT.O.) GO TO 2

ENSURE TIME LAG HAS PASSED BEFORE PLANE MOVES.

13-0. 1F(14.LE.1LAGS) GO TO 8 IF MAX DIVE/ASCENT ANGLE IS EXCEEDED, TAKE CORRECTIVE ACTION.

IF((ATHETA.GE.MAXANG).AND.(THETA.LE.O.)) GO TO 5 IF(DELS.GT.ADEL3) GO TO 6 DELS-DELS+DELTA

ENSURE MAX ORDERLD PLANE ANGLE IS NOT EXCEEDED.

ENSURE TIME LAG HAS PASSED BEFORE PLANE MOVES.

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AS ERROR SIGNAL GROWS SMALLER, THE PLANE ANGLE CAN BE REDUCED.
                                                                                                                                                        IF MAX DIVE/ASCENT ANGLE IS EXCEEDED, TAKE CORRECTIVE ACTION.
                                                                                                                                                                                                  IF((ATHETA.GE.MAXAMG).AMD.(THETA.GE.O.)) GO TO 4
IF(UABS(DELS).GT.ADEL3) GO TO 7
DELS+DELS-UELIA
                                                                                                                                                                                                                                                                                    ENSURE MAX ONDERED PLANE ANGLE IS NOT EXCLEDED.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                         ENSURE TIME LAG HAS PASSED BEFORE PLANE MOVES.
                                                        ENSUME TIME LAG HAS PASSED BEFORE PLANE MOVES.
                                                                                                                                                                                                                                                                                                                              1F (UABS (UELS). GE.STENNIX) DELS*-STENNIX
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      IF (DELTB.LE.DELTA) DELS-ADEL3
IF (DELTB.GT.DELTA) DELS-DELS-DELTA
1 1F(DELS.GE.STERMX) DELS+STERMX
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          IF(17.LE.TLAGS) GO TO 10
                                                                                                                         IF(13.1£.71A6S) GO TO 9
                                                                                                                                                                                                                                                                                                                                                                                                                    UELS-UELS-UELTA
CO TO 3
                                                                                                                                                                                                                                                                                                                                                                            DELS-DELS+DELTA
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      Se 01 00
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                          $23
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AS ERROR STUMAL GROWS SMALLER, THE PLANE ANGLE CAN BE REDUCED.
                                                                                                                                                                                                                                                                                                                                                                                                                                                              ENSURE TIME LAG IMS PASSED BEFORE PLANE MOVES.
                                                                                                                                                                                                                                                                                                              ENSURE TIME LAG HAS PASSED BEFORE PLAKE MOVES.
                                                                     IF (DELTB.LE.DELTA) DELS*-ADEL3
IF (DELTB.GT.DELTA) DELS*DELS*DELTA
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    IF(T9.LE.TLAGS) GO TO 16
IF(UELS+DELTA).GT.O.) GO TO 15
DELS=DELS+DELTA
                                                                                                                                                                                                                                                                                                                                                                     IF(110.1E.TLAGS) GO TO 17
IF((DELS-'ELTA).LT.O.) GO TO 15
1F (TB.Lt. TLAGS) GO TO 11
                                                                                                                                                                                                                                                                            IF (UELS.LT.0.) GO TO 14
                                                                                                                                                                                                                                                                                                                                                                                                      20 DELS-DELS-DELTA
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B.3 LEQTIF

- input matrix of dimension N by N containing the coefficient matrix of the equation AX = B.

On output, A is replaced by the LU decomposition of a rowwise permutation of A.

H - number of right-hand sides. (input)

N - order of A and number of rows in B. (input)

IA - number of rows in the dimension statement for A and B in the calling program. (input)

a input matrix of dimension N by M containing right-hand sides of the equation AX = B.
 On output, the N by M solution 4 replaces B.

IDGT - input sption.

If IDGT is greater than J the elements of A and B are assumed to be correct to IDGT Decimal digits and the routine performs an accuracy test.

If IDGT equals zero, the accuracy test is bypassed.

wKAREA - work area of dimension greater than or equal to N.

IER - error parameter

terminal error = 128 + N

N = 1 indicates that A is algorithmically singular.

Warning error = 32 + N.

N=2 indicates that the accuracy test failed. The computed solution may be in error by more than can be accounted for by the uncertainty of the data.

CALL LEGIT (A, M, N, IA, B, IDGT, HKAREA, IER)